

Duluth Firemen's Relief Association

Annual Actuarial Valuation
December 31, 1987

Gabriel, Roeder, Smith & Company Actuaries & Consultants

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May 18, 1988

Board of Trustees Duluth Firemen's Relief Association Duluth, Minnesota

Submitted in this report are the results of the December 31, 1987 actuarial valuation of the assets, actuarial values and contribution requirements associated with the benefits provided by the Duluth Firemen's Relief Association.

The valuation results contained in Section A provide the actuarial information needed to determine the employer's "minimum obligation" effective January 1, 1989. Section A also contains comments regarding the valuation results.

The valuation was based upon information furnished by the Association concerning benefits, financial transactions, active members, terminated members, retirants and beneficiaries. Data was checked for year to year consistency but was not otherwise audited by us. This information is summarized in Section B.

A description of the actuarial funding method and the risk experience assumptions used is contained in Section C. The economic risk experience assumptions, as well as the actuarial funding method to be used, are established by state law.

Information needed to comply with Statement No. 5 of the Governmental Accounting Standards Board is contained in Section D.

The actuarial valuation was prepared using generally accepted actuarial principles and practices based upon the methods, assumptions, summary of plan provisions and the member and financial data described in this report.

Respectfully submitted,

J. Daniel Petersen Gary W.

Section A

Valuation Results

COMMENTS

Economic Assumptions and Financing Method

The economic assumptions of 5% annual investment return and 3-1/2% annual salary increases are established by state law. State law also specifies that the annual minimum obligation of the municipality shall be determined by adding (i) the employer normal cost percent times covered payroll to (ii) the level dollar amount required to amortize the unfunded actuarial accrued liability by December 31, 2010.

It is worth noting that when the same assumptions and methods are applied to plans which differ in nature, the valuation results may not be comparable. Caution should be exercised when attempting to assess the financial condition of one Association relative to another on the basis of valuation results produced using the assumptions and methods mandated by state law.

Duluth Firemen's Relief Association

CONTRIBUTION RATE TO PROVIDE BENEFITS

Member portion & Employer portion Effective January 1, 1989

	If Paid Equally Normal Cost	Thro	oughout Year
Contributions for	% of Active Payroll for 1989	+	UAAL Dollars
Normal cost of annuities:			
Age & service: to members Age & service: to survivors Disability Death before retirement Refunds of member contributions Total Normal Cost	15.69% 2.53 2.99 1.78 0.00 22.99%		
Amortization of unfunded actuarial accrued liabilities (UAAL) (22 year level dollar payment)			
Retired lives Active members Total			\$1,137,192 1,121,997 2,259,189
Total Cost of Benefits	22.99%	+	\$2,259,189
Member contributions	8.00%		
COMPUTED EMPLOYER RATE:			
(a) If Paid Equally Throughout Year(b) IF PAID AT CALENDAR YEAR END	14.99% 15.36%	++	\$2,259,189 \$2,314,980

Duluth Firemen's Relief Association Present Actuarial Condition

The Association's accrued actuarial assets were in excess of \$11.9 million on December 31, 1987 -- a considerable sum of money if unencumbered and allocated among a small group of persons. This is not the case with the Association's assets.

The following schedule puts the \$11.9 million into perspective by showing the relationship between accrued actuarial assets, actuarial accrued liabilities, and the number of persons with actual and potential claims on the Association's assets.

	Accrued Actuarial Assets	Actuarial Accrued Liabilities	Unfunded Actuarial Accrued Liabilities	% Funded
Retirants and Beneficiaries Retired Members (107) Surviving Spouses (59) Surviving Children (4)		\$22,767,660 4,233,684 50,952		
Total (170)	\$11,842,192	\$27,052,296	\$15,210,104	43.8%
Deferred Members (1)	101,163	231,096	129,933	43.8
Active Members (109)	0	15,135,074	15,135,074	0.0
Total	\$11,943,355	\$42,418,466	\$30,475,111	28.2%

Actuarial accrued liabilities represent the value, computed as of December 31, 1987 of:

- (i) retirement allowances likely to be paid the 170 retirants and beneficiaries; and
- (ii) the contributions assumed to have been made for the 109 active members from entry into the plan until December 31, 1987.

The value of retirement allowances likely to be paid the 170 retirants and beneficiaries, discounted for investment earnings and mortality, was computed to be \$27,052,296 as of December 31, 1987. To put this amount in perspective, the \$27,052,296, together with investment earnings, will just be sufficient to pay the 170 retirants and beneficiaries their allowances for their remaining lifetimes. This assumes the 170 retirants and beneficiaries live and die according to the assumed mortality and the \$27,052,296 is invested to yield an average annual return of 5.0% over the remaining lifetimes of the retirants and beneficiaries.

With respect to the active members, the actuarial accrued liability of \$15,135,074 represents the amount that would have been accumulated by December 31, 1987. This assumes the normal cost (which is expressed as a level percentage of pay) had been contributed from the date of hire until December 31, 1987 for the 109 actives, and that these amounts had earned 5.0% interest. It also assumes that the members in the past had lived, died, withdrawn, retired and received salary increases according to the actuarial assumptions shown in this report.

Historical Funding Ratio Schedule (\$ in thousands)

Valuation Date December 31	Actuarial Accrued Liabilities	Accrued Actuarial Assets	Percent Funded
1978	\$23,066	\$ 2,045	8.9%
1979	26,232	2,605	9.9
1980	28,494	3,179	11.2
1981	31,162	3,179	10.2
1982	33,105	4,844	14.6
1983	33,747	6,886	20.4
1983*	36,360	6,886	18.9
1984	37,908	8,388	22.1
1985	40,116	9,982	24.9
1986	41,645	10,509	25.2
1987	42,418	11,943	28.2

^{*} After change in assumptions.

Duluth Firemen's Relief Association

Computed Contributions - Comparative Schedule

Year E December Valuation	er 31	Total Normal Cost as a Percent of Valuation Payroll*	Contribution For Unfunded Actuarial Accrued Liabilities \$ or %
1978	1980	21.51%	\$1,025,714
1979	1981	21.85	1,499,925
1980	1982	23.53	1,631,490
1981	1983	23.50	1,832,851
1982	1984	23.41	1,883,287
1983	1985	23.38	1,823,297
1983	1985**	25.65	2,000,666
1984	1986	24.49	2,043,837
1985	1987	23.07	2,131,035
1986	1988	23.00	2,252,482
1987	1989	22.99	2,259,189

^{*} Includes employee contributions.

^{**} After change in assumptions.

Duluth Firemen's Relief Association CONTRIBUTION FOR CALENDAR YEAR EFFECTIVE JANUARY 1, 1989

For any period of time the percent-of-payroll contribution rate is converted to dollars. The amount of dollars for any calendar year depends upon the results of the last actuarial valuation, and the timing of contributions within the year. The later the contribution date, the greater the dollar amount will be.

The municipality's dollar contribution for the year may be determined as follows:

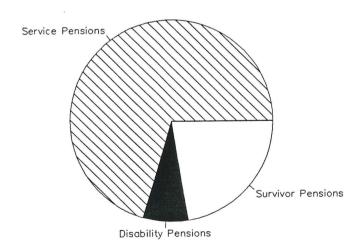
(1)	Estimated covered payroll for 1989	\$	
(2)	Total normal cost % from page A-2	22.99%	
(3)	Total normal cost (Line 1 times line 2)		\$
(4)	x 1.035 1987 Administrative expenses paid from the Special Fund		
(5)	Amortization payment on UAAL from page A-2		2,259,189
(6)	Total contributions required (Line 3 plus line 4 plus line 5)		
(7)	Employee contributions (Line 1 times 8%)	\$	
(8)	(a) State amortization aid based on 12/31/78 UAAL of \$21,020,885 \$316,364 (b) State amortization aid based on 1984 legislation 47,392 (c) Total State amortization aid	363 , 756	
(9)	Estimated insurance premium aid		
(10)	Estimated total contributions from other sources (Line 7 plus line 8 plus line 9)		
(11)	Employer's Minimum Obligation if payment is made in equal installments throughout the year (Line 6 minus line 10)		\$
(12)	EMPLOYER'S MINIMUM OBLIGATION IF PAYMENT IS MADE AT YEAR END (Line 11 times 1.0247)		\$

Section B

Valuation Data and Summary of Benefit Provisions

Duluth Firemen's Relief Association Retirants and Beneficiaries December 31, 1987 By Type of Annuity Being Paid

Type of Annuity Being Paid	No.	Monthly Amounts	Computed Actuarial Accrued Liabilities
Retirants receiving: Age & Service Disability Totals	97 10 107	\$122,181.20 12,650.00 134,831.20	\$18,976,140 3,791,520 22,767,660
Beneficiaries receiving: Spouse Child	59 4	37,905.02 1,027.93	4,233,684 50,952
Totals	63	38,932.95	4,284,636
Totals	170	\$173,764.15	\$27,052,296



Monthly Amount Paid by Benefit

Duluth Firemen's Relief Association Inactive Members Eligible for Deferred Benefits December 31, 1987

		Computed Actuarial
No.	Monthly Amount	Accrued Liabilities
1	\$1,023,11	\$231,096

Duluth Firemen's Relief Association

Retirants and Beneficiaries December 31, 1987

By Attained Ages

		Number	
Attained Ages	Age & Service	<u>Disability</u>	Death Before Retirement
Under 20			3
20-24 35-39	1	1	
40-44 45-49		2 7	1
50-54 55-59	10 11	,	1 2
60-64 65-69 70-74	15 18 37		1
75-79	22		4
80-84 85-89 90-94	10 11 7		2
95-99			_2
Totals	144	10	16

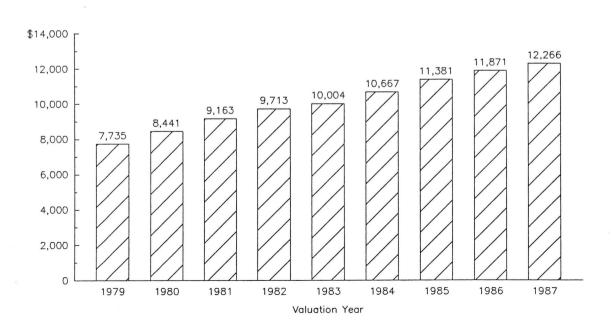
Duluth Firemen's Relief Association

Retirants and Beneficiaries Added to and Removed from Rolls

Comparative Statement

Valuation Date December 31	No. Added to Rolls	No. Removed from Rolls	<u>No.</u>	End of Year Annual Allowances	Discounted Value of Total Allowances
1978			163	\$1,078,400	\$12,763,263
1979	9	4	168	1,299,408	14,991,336
1980	9	15	162	1,367,448	15,734,056
1981	10	10	162	1,484,365	16,748,063
1982	4	4	162	1,573,451	17,422,695
1983	8	6	164	1,640,724	19,929,685
1984	8	5	167	1,781,351	21,198,961
1985	16	5	178	2,025,764	25,715,364
1986	9	14	173	2,053,628	26,708,316
1987	12	15	170	2,085,170	27,052,296

Average Annual Allowances



Duluth Firemen's Relief Association
Active Members December 31, 1987
By Attained Age and Years of Service

Attained Age	0-4	Years 5-9	of Serv 10-14	ice to 15-19	Valuati 20-24	on Date 25-29	30 Plus	No		s luation ayroll
30-34 35-39		9 10	2 9	3				11 22	\$	339,218 678,436
40-44 45-49 50-54 55-59		1	12 1	18 10 1	11 4	8	2	31 23 13 5		955,978 709,274 400,894 154,190
60 62 63 64							1 1 1 1	1 1 1		30,838 30,838 30,838 30,838
Totals		21	24	32	15	11	6	109	- \$3	,361,342

While not used in the financial computations, the following group averages are computed and shown because of their general interest.

Age: 43.7 years.

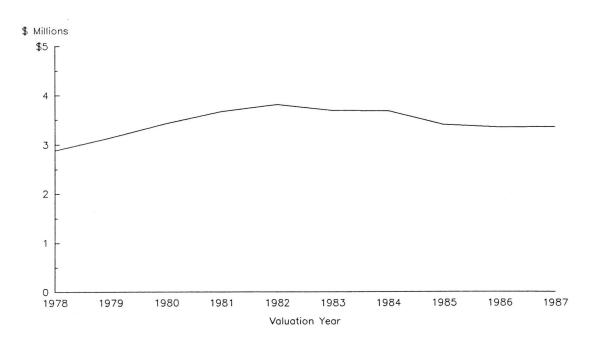
Service: 17.7 years.

Annual Pay: \$30,838.

Duluth Firemen's Relief Association Comparative Schedule Of Active Members

	Valuation		Averag	ie	
Active Members	Payroll	Age	Service	Pay	% Incr.
153	\$2,882,520	41.1 yrs.	14.7 yrs.	\$18,840	- %
153	3,143,232	40.7	14.3	20,544	9.0
153	3,425,976	40.2	13.7	22,392	9.0
150	3,670,200	40.9	14.5	24,468	9.3
147	3,812,004	41.5	15.2	25,932	6.0
140	3,687,600	42.0	15.7	26,340	1.6
133	3,683,568	42.4	16.3	27,696	5.1
118	3,405,480	42.3	16.3	28,860	4.2
112	3,353,280	42.9	16.9	29,940	3.7
109	3,361,342	43.7	17.7	30,838	3.0
	153 153 153 150 147 140 133 118	Active Members Payroll 153 \$2,882,520 153 3,143,232 153 3,425,976 150 3,670,200 147 3,812,004 140 3,687,600 133 3,683,568 118 3,405,480 112 3,353,280	Active Members Payroll Age 153 \$2,882,520 41.1 yrs. 153 3,143,232 40.7 153 3,425,976 40.2 150 3,670,200 40.9 147 3,812,004 41.5 140 3,687,600 42.0 133 3,683,568 42.4 118 3,405,480 42.3 112 3,353,280 42.9	Active Members Payroll Age Service 153 \$2,882,520 41.1 yrs. 14.7 yrs. 153 3,143,232 40.7 14.3 153 3,425,976 40.2 13.7 150 3,670,200 40.9 14.5 147 3,812,004 41.5 15.2 140 3,687,600 42.0 15.7 133 3,683,568 42.4 16.3 118 3,405,480 42.3 16.3 112 3,353,280 42.9 16.9	Active Members Payroll Age Service Pay 153 \$2,882,520 41.1 yrs. 14.7 yrs. \$18,840 153 3,143,232 40.7 14.3 20,544 153 3,425,976 40.2 13.7 22,392 150 3,670,200 40.9 14.5 24,468 147 3,812,004 41.5 15.2 25,932 140 3,687,600 42.0 15.7 26,340 133 3,683,568 42.4 16.3 27,696 118 3,405,480 42.3 16.3 28,860 112 3,353,280 42.9 16.9 29,940

Valuation Payroll



Duluth Firemen's Relief Association

Brief Summary (12/31/87) of Benefit Provisions Evaluated and/or Considered

Age & Service Retirement

Eligibility. 20 years of service and 50 years of age.

Amount. For first 20 years of service, 31.85/80 of base pay. For the 21st year, 1/80 is added. For years in excess of 21, an additional 2/80 is added up to a maximum of 40.85/80 of base pay for 25 or more years of service.

<u>Pay Used For Plan Purposes</u>. "Base pay" means the maximum pay of a firefighter on which benefits are based.

<u>Disability</u>. Disabled to the extent that unable to perform the duties of a firefighter.

Amount.

Duty Disability. 40.85/80 of base pay.

Non-Duty Disability. From 31.85/80 to 40.85/80 of base pay. (Determined by Board.)

Member's Death While Active, Or In Deferred Status, Or Retired

Eligibility.

Spouse. Legally married to member at least one year at time of separation and residing with member at time of death. Benefits terminate upon remarriage but may be reinstated if marriage terminates.

<u>Child</u>. Younger than age 18, or if full time student, younger than age 22.

Amount.

Spouse. 20/80 of base pay.

Child. 8/80 of base pay per child.

Maximum Family Benefit. 40/80 of base pay.

<u>Vested Deferred</u>. 20 years of service and separated before age 50. Payment beginning is deferred to attainment of age 50.

<u>Post-Retirement Adjustments ("Escalator")</u>. Each time base pay is changed, payments to all benefit recipients are simultaneously changed by the same percent that base pay changed.

Member Contributions. 8% of base pay. Non-refundable.

Section C

Valuation Methods and Assumptions

Duluth Firemen's Relief Association Valuation Methods and Assumptions

The Entry Age Normal Cost method was used to determine the normal cost of all benefits. The rate of investment return (interest) as required by state law used in making the valuation was 5.0 percent per annum, compounded annually. Age & service retirement was assumed to occur at age 58, or attained age if older.

Mortality Table*

Single Life Values:

	Pres	chly				
	Lev	re1	Increasing		Future Life	
Sample	For L	For Life		/early	Expectancy (Years)	
Ages	Men	Women	Men	Women	Men	Women
45	\$177.21	\$189.58	\$280.82	\$314.75	29.50	34.00
50	163.12	177.21	246.55	280.82	25.20	29.50
55	147.50	163.12	212.60	246.55	21.16	25.20
60	130.52	147.50	179.49	212.60	17.42	21.16
65	112.87	130.52	148.28	179.49	14.05	17.42
70	95.20	112.87	119.70	148.28	11.09	14.05
75	77.77	95.20	93.83	119.70	8.52	11.09
80	61.71	77.77	71.69	93.83	6.39	8.52

^{*} UP-1984 Table set forward 2 years for males and set back 3 years for females.

Sample Rates of Separation from Active Employment
Before Retirement, Death or Disability

Sample	% of Active Members
Ages	Separating within Next Year
20	1.50%
25	1.25
30	1.00
35	0.75
40	0.50
45	0.25
50+	0.00

Sample Ages	Present Pay Resulting in Pay of \$1,000 at Age 60	Present Increase in Pay During Next Year
20	\$ 253	3.5%
25	300	3.5
30	356	3.5
35	423	3.5
40	503	3.5
45	597	3.5
50	709	3.5
55	842	3.5
60	1,000	3.5

Use of the pay adjustment factor illustrated above is required by state law.

Anticipated Disability Retirements

Sample	% of Active Members Becoming
Ages	Disabled within Next Year
20	0.08%
25	0.08
30	0.08
35	0.08
40	0.20
45	0.26
50	0.49
55	0.89

Section D

The Pension Benefit Obligation and Certain Other Disclosures Required by Statement No. 5 of the Governmental Accounting Standards Board

PENSION BENEFIT OBLIGATION

The amount shown below as the "pension benefit obligation" is a standardized disclosure measure of the present value of pension benefits, adjusted for the effects of projected salary increases, estimated to be payable in the future as a result of employee service to date. The measure is the actuarial present value of credited projected benefits and is intended to (i) help users assess the plan's funding status on a going-concern basis, (ii) assess progress being made in accumulating sufficient assets to pay benefits when due, and (iii) allow for comparisons among public employee retirement plans. The measure is independent of the actuarial funding method used to determine contributions to the plan.

The pension benefit obligation was determined as part of an actuarial valuation of the plan as of December 31, 1987. Significant actuarial assumptions used in determining the pension benefit obligation include (a) a rate of return on the investment of present and future assets of 5.0% per year compounded annually, (b) projected salary increases of 3.5% per year compounded annually, attributable to inflation, and (c) the assumption that benefits will increase 3.5% per year after retirement.

At December 31, 1987, the unfunded pension benefit obligation was \$29,405,178, determined as follows:

Pension Benefit Obligation:

Retirees and beneficiaries currently receiving benefits and terminated employees not yet receiving benefits	\$27,283,392
Current employees	
Accumulated employee contributions including allocated investment income	0
Employer financed	14,123,882
Total Pension Benefit Obligation	\$41,407,274
Net assets available for benefits, at cost (market value was \$11,825,872)	12,002,096
Unfunded Pension Benefit Obligation	\$29,405,178

The total pension benefit obligation as of January 1, 1987 was \$40,650,455. During the year, the plan experienced a net change of \$756,819 in the pension benefit obligation.

CONTRIBUTIONS REQUIRED AND CONTRIBUTIONS MADE

The Association's funding policy provides for periodic employer contributions at actuarially determined rates that, expressed as percentages of annual covered payroll, are designed to accumulate sufficient assets to pay benefits when due. The normal cost and actuarial accrued liability are determined using an entry age actuarial funding method. Unfunded actuarial accrued liabilities are being amortized as a level dollar amount over a period of 22 years.

During the year ended December 31, 1987, contributions totaling \$2,942,815 -- \$2,678,944 employer and \$263,871 employee -- were made in accordance with contribution requirements determined by an actuarial valuation of the plan as of December 31, 1985. The employer contributions consisted of \$513,206 for normal cost and \$2,165,738 for amortization of the unfunded actuarial accrued liability. Employer contributions represented 78.7% of covered payroll.

Significant actuarial assumptions used to compute contribution requirements were the same as those used to compute the standardized measure of the pension benefit obligation.

Computed Contribution Comparative Schedule

Contribution Rates							
Fiscal	Valuation	Normal Cost			Dollar Con	tribution	
Year	Date	% of Valuation	UAAL	Valuation	For Fisc	al Year	
December 31	December 31	Payroll	Dollars	Payroll	Computed	Actual	
1987	1985	15.07%	\$2,131,035	\$3 , 405 , 480	\$2,644,241	\$2 , 678 , 944	
1988	1986	15.00	2,252,482	3,353,280	2,755,474		
1989	1987	14.99	2,259,189	3,361,342	2,763,054		

REQUIRED SUPPLEMENTARY INFORMATION ANALYSIS OF FUNDING PROGRESS

		(2)				(6)
	(1)	Pension	(3)	(4)	(5)	Unfunded PBO
Valuation	Net Assets	Benefit	Percent	Unfunded	Annual	as a Percentage
Date	Available	Obligation 0	Funded	PB0	Covered	of Covered Payroll
December 31	for Benefits	(PBO)	(1)/(2)	(2)-(1)	Payroll	(4)/(5)
1987	\$12,002,096	\$41,407,274	29.0%	\$29,405,178	\$3,361,342	874.8%

Analysis of the dollar amounts of net assets available for benefits, pension benefit obligation, and unfunded pension benefit obligation in isolation can be misleading. Expressing the net assets available for benefits as a percentage of the pension benefit obligation provides one indication of the plan's funded status on a going-concern basis. Analysis of this percentage over time indicates whether the system is becoming financially stronger or weaker. Generally, the greater this percentage, the stronger the plan. The unfunded pension benefit obligation and annual covered payroll are both affected by inflation. Expressing the unfunded pension benefit obligation as a percentage of annual covered payroll approximately adjusts for the effects of inflation and aids analysis of the progress being made in accumulating sufficient assets to pay benefits when due. Generally, the smaller this percentage, the stronger the plan.

Appendices

APPENDIX I

FINANCIAL PRINCIPLES AND OPERATIONAL TECHNIQUES

Promises Made, and Eventually Paid. As each year is completed, the plan in effect hands an "IOU" to each member then acquiring a year of service credit -- the "IOU" says: "The Pension Plan owes you a portion of your retirement benefits, payments to be made in cash, commencing when you qualify for retirement."

The related key financial questions are: Which generation of taxpayers contributes the money to cover the IOU? The present taxpayers, who receive the benefit of the member's present year of service? Or the future taxpayers, who happen to be in town paying taxes at the later time when the IOU becomes a cash demand?

A sound principle of sound retirement plan financing is to have this year's taxpayers contribute the money to cover the IOUs being handed out this year. By following this principle, THE CONTRIBUTION RATE WILL REMAIN APPROXIMATELY LEVEL FROM GENERATION TO GENERATION -- our children and grandchildren will contribute the same percents of active payroll we contribute now.

A PENSION PLAN BECOMES CLOSED

The diagram in this appendix shows two important activities which occur after a plan has been closed to employees hired in the future.

Cash benefits paid continue to increase for decades, while active member payroll begins to decrease to zero. <u>Funding Method</u>. A funding method is the long-term, planned pattern for employer contributions.

For an open plan (a plan covering future employees), the level-percent-of-active-member payroll funding method is the basic funding method.

The level-percent funding method can also be applied to a closed plan. However, the resulting contribution percent usually jumps to a high rate, because the number of covered active members is decreasing.

A preferred funding method for a closed plan consists of: level-percent funding for normal cost (the cost of members' service now being rendered); plus a level dollar contribution for unfunded actuarial accrued liabilities over a limited period of years. The period of years must be limited so that plan assets don't become zero while benefits are still payable.

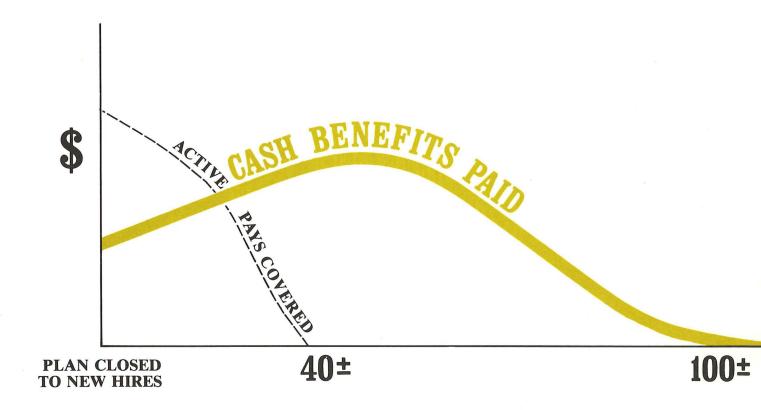
Computing Contributions To Support Plan Benefits. From a given schedule of benefits and from the employee data and asset data furnished him, the actuary determines the contribution rates to support the benefits by means of an actuarial valuation and a funding method.

In making an actuarial valuation, assumptions must be made regarding anticipated financial experiences for the next year and for decades in the future. Only the subsequent actual experience of the plan can indicate the degree of accuracy of the assumptions.

Reconciling Differences Between Assumed Experience and Actual Experience. Once actual experience has occurred and been observed, it will not coincide exactly with assumed experience, regardless of the wisdom of the assumptions or the skill of the actuary and the millions of calculations he made. The future can be predicted with considerable but not 100% precision, except for inflation which seems to defy reliable prediction.

A well-managed plan copes with these continually changing differences by having periodic actuarial valuations. Each actuarial valuation is a complete recalculation of assumed future experience, taking into account all past differences between assumed and actual experience. The result is continuing adjustment in financial position.

A CLOSED PENSION PLAN



YEARS OF TIME

A plan becomes closed when no new hires are admitted to active membership. The persons covered by the plan at the time of closing continue their normal activities and continue to be covered by the plan, until the last survivor dies.

CASH BENEFITS LINE. After a pension plan becomes closed, the usual pattern is for cash benefits to continue to increase for decades of time. Eventually the cash benefits will peak, and then gradually decrease over more decades of time, ultimately to zero. The last cash benefit is likely to occur a century after the time the plan is closed.

The precise amounts of cash benefits cannot be known now, and must be estimated by assumptions of future experiences in a variety of financial risk areas.

APPENDIX II

MEANING OF UNFUNDED ACCRUED LIABILITIES

Almost every pension plan (public or private) has "unfunded accrued liabilities", so whatever they are, they aren't rare. Since the term is not part of everyday conversation, it needs some definition.

"Accrued liabilities" are the present value \$ of plan promises to pay benefits in the future based upon service already rendered - - - a liability has been established ("accrued") because the service has been rendered, but the resulting monthly cash benefit may not be payable until years in the future. Accrued liabilities \$ are the result of complex mathematical calculations, which are made by the plan's actuary (which is the name given to the specialist who makes such calculations).

If "accrued liabilities" at any time exceed the plan's accrued assets (cash & investments), the difference is "unfunded accrued liabilities". This is the common condition. If the plan's assets equalled the plan's "accrued liabilities", the plan would be termed "fully funded". This is a rare condition.

Each time a plan adds a new benefit which applies to service already rendered, an "accrued liability" is created, which is also an "unfunded accrued liability" because the plan can't print instant cash to cover the accrued liability. Payment for such unfunded accrued liabilities is spread over a period of years, commonly in the 20-40 year range.

Unfunded accrued liabilities can occur in another way: If actual financial experience is less favorable than assumed financial experience, the difference is added to unfunded accrued liabilities. In plans where plan benefits are directly related to an employee's pay near time of retirement (a common plan provision) rather than his average pay throughout his working career, unfunded accrued liabilities have been increasing in recent years because unexpected rates of pay increase have created additional accrued liabilities which could not be matched by reasonable investment results. Some of these unexpected pay increases are the direct result of inflation, which is a very destructive force on financial stability.

The existence of unfunded accrued liabilities is not bad, then (any more than a mortgage on your house is "bad"), but the changes from year to year in amount of unfunded accrued liabilities are important - - - "bad" or "good" or somewhere in between.

Nor are unfunded accrued liabilities a bill payable immediately (your food costs are payable immediately), but it is important that policy-makers prevent the amount from becoming unreasonably high and it is vital that your plan have a sound method for making payments toward them so that they are controlled.

The existence of large amounts of unfunded accrued liabilities indicates that total contributions in past years were less than level - - - an almost certain history if retired life liabilities are not fully funded now.