# R $\begin{aligned} & \text { Gabriel Roeder Smith } \& \text { Consultants \& Actuaries }\end{aligned}$ Consultants \& Actuaries 

December 19, 2016

St. Paul Teachers' Retirement Fund Association
1619 Dayton Avenue, Room 309
St. Paul, Minnesota 55104-6206

## Dear Trustees:

This report provides accounting and financial reporting information that is intended to comply with the Governmental Accounting Standards Board (GASB) Statement Nos. 67 and 68 for the St. Paul Teachers' Retirement Fund Association ("SPTRFA" or "Fund"). These calculations have been made on a basis that is consistent with our understanding of these Statements.

GASB Statement No. 67 is the accounting standard that applies to the stand-alone financial reports issued by retirement systems. GASB Statement No. 68 establishes accounting and financial reporting for state and local government employers who provide their employees (including former employees) pension benefits through a trust.

Our calculation of the liability associated with the benefits described in this report was performed for the purpose of providing reporting and disclosure information that satisfies the requirements of GASB Statement Nos. 67 and 68. The Net Pension Liability is not an appropriate measure for measuring the sufficiency of plan assets to cover the estimated cost of settling the employer's benefit obligation. The Net Pension Liability is not an appropriate measure for assessing the need for or amount of future employer contributions. The calculation of the plan's liability for this report is not applicable for funding purposes of the plan. A calculation of the plan's liability for purposes other than satisfying the requirements of GASB Statement No. 67 may produce significantly different results. The information in this report is calculated on a total plan basis. The Fund is responsible for preparing the Schedule of Employer Allocations and the Schedule of Pension Amounts by Employer. This report may be provided to parties other than the St. Paul Teachers' Retirement Fund Association only in its entirety and only with the permission of the Board. GRS is not responsible for unauthorized use of this report.

This report is based upon information, furnished to us by the Fund, concerning retirement and ancillary benefits, active members, deferred vested members, retirees and beneficiaries, and financial data. If your understanding of this information is different, please let us know. This information was checked for internal consistency, but it was not audited.

This report complements the actuarial valuation report for funding purposes that was or will be provided to the System and should be considered in conjunction with that report. Please see the actuarial valuation report as of June 30, 2016 for additional discussion of the nature of actuarial calculations and more information related to participant data, economic and demographic assumptions, and benefit provisions.

To the best of our knowledge, the information contained within this report is accurate and fairly represents the actuarial position of the St. Paul Teachers' Retirement Fund Association. All calculations have been made in conformity with generally accepted actuarial principles and practices as well as with the Actuarial Standards of Practice issued by the Actuarial Standards Board.

St. Paul Teachers' Retirement Fund Association
December 19, 2016
Page 2

The signing actuaries are independent of the plan sponsor.
Bonita J. Wurst and James D. Anderson are Members of the American Academy of Actuaries (MAAA) and meet the Qualification Standards of the American Academy of Actuaries to render the actuarial opinions contained herein.

Respectfully submitted,


Bonita J. Wurst, ASA, EA, FCA, MAAA


BJW/JDA:bd

## Table of Contents

Page
Section A Executive Summary
Executive Summary ..... 1
Discussion ..... 2-4
Section B Financial Statements
Statement of Pension Expense ..... 5
Statement of Outflows and Inflows Arising from Current Period ..... 6
Statement of Outflows and Inflows Arising from Current and Prior Periods ..... 7
Statement of Fiduciary Net Position ..... 8
Statement of Changes in Fiduciary Net Position ..... 9
Section C Required Supplementary Information
Schedule of Changes in Net Pension Liability and Related Ratios Current Period ..... 10
Schedule of Changes in Net Pension Liability and Related Ratios Multiyear. ..... 11
Schedule of Net Pension Liability Multiyear ..... 12
Schedule of Contributions Multiyear ..... 13
Notes to Schedule of Contributions ..... 13
Schedule of Investment Returns Multiyear. ..... 14
Section D Notes to Financial Statements
Asset Allocation ..... 15
Sensitivity of Net Pension Liability to the Single Discount Rate Assumption ..... 16
Reconciliation of Members ..... 17
GASB Reconciliation ..... 18
Section E Summary of Benefits ..... 19-26
Section F Actuarial Cost Method and Actuarial Assumptions
Valuation Methods, Entry Age Normal ..... 27
Actuarial Assumptions, Input to Discount Rates, Mortality Assumptions, and Experience Studies ..... 28-35
Section G Calculation of the Single Discount Rate
Calculation of the Single Discount Rate ..... 36
Projection of Contributions ..... 37-38
Projection of Plan Fiduciary Net Position ..... 39-40
Present Values of Projected Benefits ..... 41-42
Section H Glossary of Terms ..... 43-46

## SECTION A <br> EXECUTIVE SUMMARY

## EXECUTIVE SUMMARY AS OF June 30, 2016 (Dollars in Thousands)

|  |  |  | 2016 |  |
| :---: | :---: | :---: | :---: | :---: |
| Actuarial Valuation Date |  |  | June 30, 2016 |  |
| Measurement Date of the Net Pension Liability |  |  | June 30, 2016 |  |
| Membership |  |  |  |  |
| Number of |  |  |  |  |
| - Service Retirements |  |  |  | 3,324 |
| - Survivors |  |  |  | 328 |
| - Disability Retirements |  |  |  | 31 |
| - Alternate Payees |  |  |  | 40 |
| - Deferred Retirements |  |  |  | 2,020 |
| - Terminated other non-vested |  |  |  | 2,915 |
| - Active Members |  |  |  | 3,534 |
| - Total |  |  |  | 12,192 |
| Covered Payroll |  |  | \$ | 258,787 |
| Net Pension Liability |  |  |  |  |
| Total Pension Liability |  |  | \$ | 1,592,570 |
| Plan Fiduciary Net Position |  |  |  | 959,666 |
| Net Pension Liability |  |  | \$ | 632,904 |
| Plan Fiduciary Net Position as a Percentage |  |  |  |  |
| Net Pension Liability as a Percentage |  |  |  |  |
| Development of the Single Discount Rate |  |  |  |  |
| Single Discount Rate |  |  |  | 8.00\% |
| Long-Term Expected Rate of Investment Return |  |  |  | 8.00\% |
| Long-Term Municipal Bond Rate* |  |  |  | 2.85\% |
| Last year ending June 30 in the 2017 to 2116 projection period within which projected benefit payments are fully funded |  |  |  | 2116 |
| Total Pension Expense |  |  | \$ | 51,314 |
| Deferred Outflows and Deferred Inflows of Resources by Source to be Recognizedin Future Pension Expenses Deferred Outflows Deferred Inflows of Resources of Resources |  |  |  |  |
| Difference between expected and actual experience | \$ | - | \$ | 48,504 |
| Changes in assumptions |  | 15,858 |  | - |
| Net difference between projected and actual earnings on pension plan investments |  | 95,338 |  | 38,304 |
| Total | \$ | 111,196 | \$ | 86,808 |

[^0]
## DISCUSSION

## Accounting Standard

For pension plans that are administered through trusts or equivalent arrangements, Governmental Accounting Standards Board (GASB) Statement No. 67 establishes standards of financial reporting for separately issued financial reports and specifies the required approach for measuring the pension liability. Similarly, GASB Statement No. 68 establishes standards for state and local government employers (as well as non-employer contributing entities) to account for and disclose the net pension liability, pension expense, and other information associated with providing retirement benefits to their employees (and former employees) on their basic financial statements.

The following discussion provides a summary of the information that is required to be disclosed under these accounting standards. A number of these disclosure items are provided in this report. However, certain information, such as notes regarding accounting policies and investments, is not included in this report and the retirement system and/or plan sponsor will be responsible for preparing and disclosing that information to comply with these accounting standards.

## Financial Statements

GASB Statement No. 68 requires state or local governments to recognize the net pension liability and the pension expense on their financial statements. The net pension liability is the difference between the total pension liability and the plan's fiduciary net position. In traditional actuarial terms, this is analogous to the accrued liability less the market value of assets (not the smoothed actuarial value of assets that is often encountered in actuarial valuations performed to determine the employer's contribution requirement).

Paragraph 57 of GASB Statement No. 68 states, "Contributions to the pension plan from the employer subsequent to the measurement date of the collective net pension liability and before the end of the employer's reporting period should be reported as a deferred outflow of resources related to pensions." There were no contributions made to SPTRFA subsequent to the measurement date of June 30, 2016.

The pension expense recognized each fiscal year is equal to the change in the net pension liability from the beginning of the year to the end of the year, adjusted for deferred recognition of the liability and investment experience.

Pension plans that prepare their own, stand-alone financial statements are required to present two financial statements - a statement of fiduciary net position and a statement of changes in fiduciary net position in accordance with GASB Statement No. 67. The statement of fiduciary net position presents the assets and liabilities of the pension plan at the end of the pension plan's reporting period. The statement of changes in fiduciary net position presents the additions, such as contributions and investment income, and deductions, such as benefit payments and expenses, and net increase or decrease in the fiduciary net position.

## Notes to Financial Statements

GASB Statement No. 68 requires the notes of the employer's financial statements to disclose the total pension expense, the pension plan's liabilities and assets, and deferred outflows and inflows of resources related to pensions.

GASB Statement Nos. 67 and 68 require the notes of the financial statements for the employers and pension plans, to include certain additional information. The list of disclosure items should include:

- a description of benefits provided by the plan;
- the type of employees and number of members covered by the pension plan;
- a description of the plan's funding policy, which includes member and employer contribution requirements;
- the pension plan's investment policies;
- the pension plan's fiduciary net position, net pension liability, and the pension plan's fiduciary net position as a percentage of the total pension liability;
- the net pension liability using a discount rate that is $1 \%$ higher and $1 \%$ lower than used to calculate the total pension liability and net pension liability for financial reporting purposes;
- significant assumptions and methods used to calculate the total pension liability;
- inputs to the discount rates; and
- certain information about mortality assumptions and the dates of experience studies.

Retirement systems that issue stand-alone financial statements are required to disclose additional information in accordance with GASB Statement No. 67. This information includes:

- the composition of the pension plan's Board and the authority under which benefit terms may be amended;
- a description of how fair value is determined;
- information regarding certain reserves and investments, which include concentrations of investments greater than or equal to $5 \%$, receivables, and insurance contracts excluded from plan assets; and
- annual money-weighted rate of return.


## Required Supplementary Information

GASB Statement No. 67 requires a 10-year fiscal history of:

- sources of changes in the net pension liability;
- information about the components of the net pension liability and related ratios, including the pension plan's fiduciary net position as a percentage of the total pension liability, and the net pension liability as a percent of covered-employee payroll; and
- a comparison of the actual employer contributions to the actuarially determined contributions based on the plan's funding policy.


## Measurement of the Net Pension Liability

The net pension liability is to be measured as the total pension liability, less the amount of the pension plan's fiduciary net position. In actuarial terms, this will be the accrued liability less the market value of assets (not the smoothed actuarial value of assets that is often encountered in actuarial valuations performed to determine the employer's contribution requirement).

## General Implications of Contribution Allocation Procedure or Funding Policy on Future Expected Plan Contributions and Funded Status

Given the plan's contribution allocation procedure, if all actuarial assumptions are met (including the assumption of the plan earning $8.00 \%$ on the actuarial value of assets), then the following outcomes are expected:

1. The unfunded actuarial accrued liabilities will increase in the short term but will be fully amortized after approximately 40 years.
2. The funded status of the plan will continue to increase towards a $100 \%$ funded ratio.

The projections in this report are strictly for the purpose of determining the GASB single discount rate and are different from a funding projection for the ongoing plan.

## Timing of the Valuation

An actuarial valuation to determine the total pension liability is required to be performed at least every two years. The net pension liability and pension expense should be measured as of the pension plan's fiscal year end (measurement date) on a date that is within the employer's prior fiscal year. If the actuarial valuation used to determine the total pension liability is not calculated as of the measurement date, the total pension liability is required to be rolled forward from the actuarial valuation date to the measurement date.

The total pension liability shown in this report is based on an actuarial valuation performed as of June 30, 2016 and a measurement date of June 30, 2016.

## Single Discount Rate

Projected benefit payments are required to be discounted to their actuarial present values using a single discount rate. This rate differs depending on whether or not the Fund has a projected sufficiency of assets to pay benefits.

Due to the projected sufficiency of assets to pay benefits, the single discount rate is equal to the $8.00 \%$ long-term expected rate of return on pension plan investments, for the purposes of this valuation.

Had the Fund been projected to have insufficient assets to pay all projected benefits, the single discount rate would instead reflect a combination of (1) the $8.00 \%$ long-term expected rate of return on pension plan investments (for all years where a projected asset sufficiency exists), then (2) a lower tax-exempt municipal bond rate* (for all remaining years where projected asset insufficiencies exist).

* Based on an index of 20-year general obligation bonds with an average AA credit rating as of the measurement date. That municipal bond rate, which was not used to discount any projected benefits in this valuation, was $2.85 \%$ (based on the weekly rate closest to but not later than the measurement date of the Bond Buyer 20-Year GO Index).


## Effective Date and Transition

GASB Statement Nos. 67 and 68 were effective for fiscal years beginning after June 15, 2013, and June 15, 2014 respectively.

## SECTION B <br> FINANCIAL STATEMENTS

Note - Section B is intended to assist in preparation of the financial statements of the St. Paul Teachers' Retirement Fund Association. Financial statements are the responsibility of management, subject to the auditor's review.

## Pension Expense Under GASB Statement No. 68 Fiscal Year Ended June 30, 2016 (Dollars in Thousands)

A. Expense/(Income)

1. Service Cost ..... \$ 25,5963. Current-Period Benefit Changes
2. Employee Contributions (made negative for addition here)5. Projected Earnings on Plan Investments (made negative for addition here)6. Pension Plan Administrative Expense7. Other Changes in Plan Fiduciary Net Position8. Recognition of Outflow (Inflow) of Resources due to Liabilities
3. Interest on the Total Pension Liability124,2949. Recognition of Outflow (Inflow) of Resources due to Assets$(18,538)$10. Total Pension Expense / (Income)$(78,926)$
7490$(9,324)$
7,463
\$ 51,314

# Statement of Outflows and Inflows Arising from Current Reporting Period <br> Fiscal Year Ended June 30, 2016 (Dollars in Thousands) 

## A. Outflows (Inflows) of Resources due to Liabilities

1. Difference between expected and actual experience
of the Total Pension Liability (gains) or losses
\$
2. Assumption Changes (gains) or losses
\$
3. Recognition period for Liabilities: Average of the expected remaining service lives of all employees \{in years \}
4. Outflow (Inflow) of Resources to be recognized in the current pension expense for the difference between expected and actual experience of the Total Pension Liability*
\$
$(10,574)$
5. Outflow (Inflow) of Resources to be recognized in the current pension expense for
Assumption Changes
6. Outflow (Inflow) of Resources to be recognized in the current pension expense due to Liabilities
\$
$(10,574)$
7. Deferred Outflow (Inflow) of Resources to be recognized in future pension expenses for the difference between expected and actual experience of the Total Pension Liability
\$
8. Deferred Outflow (Inflow) of Resources to be recognized in future pension expenses for Assumption Changes
9. Deferred Outflow (Inflow) of Resources to be recognized in future pension expenses due to Liabilities

## B. Outflows (Inflows) of Resources due to Assets

1. Net difference between projected and actual earnings on pension plan investments (gains) or losses \$

$$
77,451
$$

2. Recognition period for Assets \{in years \} 5.0000
3. Outflow (Inflow) of Resources to be recognized in the current pension expense due to Assets
4. Deferred Outflow (Inflow) of Resources to be recognized in future pension expenses due to Assets
\$
61,961
[^1]
## Statement of Outflows and Inflows Arising from Current and Prior Reporting Periods

Fiscal Year Ended June 30, 2016 (Dollars in Thousands)
A. Outflows and Inflows of Resources due to Liabilities and Assets to be Recognized in Current Pension Expense

|  | Outflows of Resources |  | Inflows of Resources |  | Net Outflows of Resources |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. Due to Liabilities | \$ | 7,928 | \$ | 17,252 | \$ | $(9,324)$ |
| 2. Due to Assets |  | 26,616 |  | 19,153 |  | 7,463 |
| 3. Total | \$ | 34,544 | \$ | 36,405 | \$ | $(1,861)$ |

B. Outflows and Inflows of Resources by Source to be Recognized in Current Pension Expense

|  | Outflows of Resources |  | Inflows of Resources |  | Net Outflows of Resources |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. Differences between expected and actual experience | \$ | - | \$ | 17,252 | \$ | $(17,252)$ |
| 2. Assumption Changes |  | 7,928 |  | - |  | 7,928 |
| 3. Net Difference between projected and actual earnings on pension plan investments |  | 26,616 |  | 19,153 |  | 7,463 |
| 4. Total | \$ | 34,544 | \$ | 36,405 | \$ | $(1,861)$ |

C. Deferred Outflows and Deferred Inflows of Resources by Source to be Recognized in Future Pension Expenses

|  | Deferred Outflows of Resources |  | Deferred Inflows of Resources |  | Net Deferred Outflows of Resources |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. Differences between expected and actual experience | \$ | - | \$ | 48,504 | \$ | $(48,504)$ |
| 2. Assumption Changes |  | 15,858 |  | - |  | 15,858 |
| 3. Net Difference between projected and actual earnings on pension plan investments |  | 95,338 |  | 38,304 |  | 57,034 |
| 4. Total | \$ | 111,196 | \$ | 86,808 | \$ | 24,388 |

D. Deferred Outflows and Deferred Inflows of Resources by Year to be Recognized in Future Pension Expenses

| Year Ending <br> June 30 |  | Net Deferred Outflows <br> of Resources |
| :---: | :---: | :---: |
|  |  | $(1,861)$ |
| 2017 | $\$$ | $(1,859)$ |
| 2019 |  | 12,616 |
| 2020 |  | 15,492 |
| 2021 |  | - |
| Thereafter |  | 0 |
| Total | $\$$ | 24,388 |

# Statement of Fiduciary Net Position as of June 30, 2016 (Dollars in Thousands) 

## Assets

Cash and Deposits
Receivables
Accounts Receivable - Sale of Investments
Accrued Interest and Other Dividends
Contributions
Accounts Receivable - Other
Total Receivables
Investments

| Fixed Income | \$ | 179,666 |
| :---: | :---: | :---: |
| Equities |  | 585,065 |
| Real Estate |  | 71,970 |
| Other |  | 79,380 |
| Total Investments | \$ | 916,081 |
| Total Assets | \$ | 961,822 |

Total Assets
2016
-
\$ 45,741


## Liabilities

Payables

| Accounts Payable - Purchase of Investments | $\$$ | 2,156 |
| :--- | :---: | :---: |
| Accrued Expenses |  | - |
| Accounts Payable - Other |  | - |
| Total Liabilities | $\$$ | 2,156 |
| osition Restricted for Pensions | $\$$ | 959,666 |

## Statement of Changes in Fiduciary Net Position for Year Ended June 30, 2016 (Dollars in Thousands)

| Additions |  |  |
| :---: | :---: | :---: |
| Contributions |  |  |
| Employer | \$ | 26,433 |
| Employer (for Reemployed Annuitants) |  | 130 |
| Employee |  | 18,538 |
| Other |  | 10,665 |
| Total Contributions | \$ | 55,766 |
| Investment Income |  |  |
| Net Appreciation in Fair Value of Investments | \$ | $(8,934)$ |
| Interest and Dividends |  | 14,033 |
| Less Investment Expense |  | $(3,624)$ |
| Net Investment Income | \$ | 1,475 |
| Other | \$ | 0 |
| Total Additions | \$ | 57,241 |
| Deductions |  |  |
| Benefit payments, including refunds of employee contributions | \$ | 111,795 |
| Pension Plan Administrative Expense |  | 749 |
| Other |  | - |
| Total Deductions | \$ | 112,544 |
| Net Increase in Net Position | \$ | $(55,303)$ |
| Net Position Restricted for Pensions |  |  |
| Beginning of Year | \$ | 1,014,969 |
| End of Year | \$ | 959,666 |

## SECTION C <br> REQUIRED SUPPLEMENTARY INFORMATION

Note - Section C is intended to assist in preparation of the financial statements of the St. Paul Teachers' Retirement Fund Association. Financial statements are the responsibility of management, subject to the auditor's review.

## Schedule of Changes in Net Pension Liability and Related Ratios Current Period

Fiscal Year Ended June 30, 2016 (Dollars in Thousands)

## A. Total pension liability

1. Service Cost
2. Interest on the Total Pension Liability
3. Changes of benefit terms
4. Difference between expected and actual experience of the Total Pension Liability ${ }^{+}$
5. Changes of assumptions
6. Benefit payments, including refunds of employee contributions
7. Net change in Total Pension Liability
8. Total Pension Liability - Beginning
9. Total Pension Liability - Ending

## B. Plan fiduciary net position

1. Contributions - Employer
2. Contributions - Employee
3. Net investment income
4. Benefit payments, including refunds of employee contributions
5. Pension Plan Administrative Expense
6. Other
7. Net change in Plan Fiduciary Net Position
8. Plan Fiduciary Net Position - Beginning
9. Plan Fiduciary Net Position - Ending
C. Net Pension Liability

## D. Plan Fiduciary Net Position as a Percentage

 of the Total Pension LiabilityE. Covered-Employee payroll
F. Net pension liability as a percentage of Covered-Employee payroll

25,596
124,294

0 $\frac{(111,795)}{(4,200)}$

|  | $(111,795)$ |
| :--- | ---: |
| $\$$ | $(4,200)$ |
|  | $1,596,770$ |
| $\$$ | $\mathbf{1 , 5 9 2 , 5 7 0}$ |

1,592,570

|  | $(111,795)$ |
| :--- | ---: |
| $\$$ | $(4,200)$ |
|  | $1,596,770$ |
| $\$$ | $\mathbf{1 , 5 9 2 , 5 7 0}$ |

$\left.\begin{array}{lr}\$ & 37,228 \\ 18,538 \\ 1,475\end{array}\right]$

## Schedules of Required Supplementary Information Schedule of Changes in Net Pension Liability and Related Ratios Multiyear (Dollars in Thousands)

## Last 10 Fiscal Years (to be completed prospectively, commencing with 2014)

| Fiscal year ending June 30, |  | 016 |  | 2015 |  | 2014 | 2013 | 2012 | 2011 | 2010 | 2009 | 2008 | 2007 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total Pension Liability |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Service Cost | \$ | 25,596 | \$ | 24,998 | \$ | 22,954 |  |  |  |  |  |  |  |
| Interest on the Total Pension Liability |  | 124,294 |  | 123,108 |  | 118,503 |  |  |  |  |  |  |  |
| Benefit Changes |  | - |  | $(5,677)$ |  | - |  |  |  |  |  |  |  |
| Difference between Expected and Actual Experience |  | $(42,295)$ |  | $(17,133)$ |  | $(16,257)$ |  |  |  |  |  |  |  |
| Assumption Changes |  | - |  | - |  | 39,642 |  |  |  |  |  |  |  |
| Benefit Payments |  | $(111,167)$ |  | $(108,878)$ |  | $(105,742)$ |  |  |  |  |  |  |  |
| Refunds |  | (628) |  | (875) |  | $(1,103)$ |  |  |  |  |  |  |  |
| Net Change in Total Pension Liability |  | $(4,200)$ |  | 15,543 |  | 57,997 |  |  |  |  |  |  |  |
| Total Pension Liability - Beginning |  | 1,596,770 |  | 1,581,227 |  | 1,523,230 |  |  |  |  |  |  |  |
| Total Pension Liability - Ending (a) | \$ | 1,592,570 | \$ | 1,596,770 | \$ | 1,581,227 |  |  |  |  |  |  |  |
| Plan Fiduciary Net Position |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Employer Contributions* | \$ | 37,228 | \$ | 36,711 | \$ | 35,197 |  |  |  |  |  |  |  |
| Employee Contributions |  | 18,538 |  | 17,567 |  | 16,564 |  |  |  |  |  |  |  |
| Pension Plan Net Investment Income |  | 1,475 |  | 25,757 |  | 168,176 |  |  |  |  |  |  |  |
| Benefit Payments |  | $(111,167)$ |  | $(108,878)$ |  | $(105,742)$ |  |  |  |  |  |  |  |
| Refunds |  | (628) |  | (875) |  | $(1,103)$ |  |  |  |  |  |  |  |
| Pension Plan Administrative Expense |  | (749) |  | (748) |  | (739) |  |  |  |  |  |  |  |
| Other |  | - |  | - |  | - |  |  |  |  |  |  |  |
| Net Change in Plan Fiduciary Net Position |  | $(55,303)$ |  | $(30,466)$ |  | 112,353 |  |  |  |  |  |  |  |
| Plan Fiduciary Net Position - Beginning |  | 1,014,969 |  | 1,045,435 |  | 933,082 |  |  |  |  |  |  |  |
| Plan Fiduciary Net Position - Ending (b) | \$ | 959,666 | \$ | 1,014,969 | \$ | 1,045,435 |  |  |  |  |  |  |  |
| Net Pension Liability - Ending (a) - (b) |  | 632,904 |  | 581,801 |  | 535,792 |  |  |  |  |  |  |  |
| Plan Fiduciary Net Position as a Percentage |  |  |  |  |  |  |  |  |  |  |  |  |  |
| of Total Pension Liability |  | 60.26 \% |  | 63.56 \% |  | 66.12 \% |  |  |  |  |  |  |  |
| Covered-Employee Payroll | \$ | 258,787 | \$ | 263,844 | \$ | 259,740 |  |  |  |  |  |  |  |
| Net Pension Liability as a Percentage |  |  |  |  |  |  |  |  |  |  |  |  |  |
| of Covered-Employee Payroll |  | 244.57 \% |  | 220.51 \% |  | 206.28 \% |  |  |  |  |  |  |  |
| Notes to Schedule: |  |  |  |  |  |  |  |  |  |  |  |  |  |
| N/A |  |  |  |  |  |  |  |  |  |  |  |  |  |

 as defined in GASB Statement Nos. $67-68$.

# SCHEDULES OF REQUIRED SUPPLEMENTARY INFORMATION <br> Schedule of the Net Pension Liability Multiyear (DOLLARS IN THOUSANDS) 

## Last 10 Fiscal Years (to be completed prospectively, commencing with 2014)

| FY Ending June 30, |  | Total ension iability |  | an Net <br> osition | Net Pension Liability |  | Plan Net Position as a \% of Total Pension Liability | Covered <br> Payroll |  | Net Pension Liability as a \% of Covered Payroll |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2007 |  |  |  |  |  | - |  |  |  |  |
| 2008 |  |  |  |  |  | - |  |  |  |  |
| 2009 |  |  |  |  |  | - |  |  |  |  |
| 2010 |  |  |  |  |  | - |  |  |  |  |
| 2011 |  |  |  |  |  | - |  |  |  |  |
| 2012 |  |  |  |  |  | - |  |  |  |  |
| 2013 |  |  |  |  |  | - |  |  |  |  |
| 2014 | \$ | 1,581,227 | \$ | 1,045,435 | \$ | 535,792 | 66.12\% | \$ | 259,740 | 206.28\% |
| 2015 |  | 1,596,770 |  | 1,014,969 |  | 581,801 | 63.56\% |  | 263,844 | 220.51\% |
| 2016 |  | 1,592,570 |  | 959,666 |  | 632,904 | 60.26\% |  | 258,787 | 244.57\% |

The covered payroll shown represents the annual compensation for active employees on which contributions to the pension plan are based and does not necessarily represent Covered Payroll as defined in GASB Statement Nos. 67-68.

## Schedule of Contributions Multiyear (Dollars in Thousands) Last 10 Fiscal Years

| FY Ending June 30, | Actuarially <br> Determined <br> Contribution |  |  | ual <br> ution* | Contribution <br> Deficiency <br> (Excess) |  | Covered <br> Payroll |  | Actual Contribution as a \% of Covered Payroll |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2007 | \$ | 42,823 | \$ | 24,117 | \$ | 18,706 | \$ | 229,172 | 10.52\% |
| 2008 |  | 41,580 |  | 24,285 |  | 17,295 |  | 235,993 | 10.29 |
| 2009 |  | 29,007 |  | 24,844 |  | 4,163 |  | 243,166 | 10.22 |
| 2010 |  | 30,328 |  | 25,126 |  | 5,202 |  | 239,996 | 10.47 |
| 2011 |  | 33,819 |  | 25,090 |  | 8,729 |  | 239,738 | 10.47 |
| 2012 |  | 29,797 |  | 25,109 |  | 4,688 |  | 239,053 | 10.50 |
| 2013 |  | 41,424 |  | 26,445 |  | 14,979 |  | 247,432 | 10.69 |
| 2014 |  | 40,916 |  | 35,197 |  | 5,719 |  | 259,740 | 13.55 |
| 2015 |  | 40,320 |  | 36,711 |  | 3,609 |  | 263,844 | 13.91 |
| 2016 |  | 39,155 |  | 37,228 |  | 1,927 |  | 258,787 | 14.39 |

* Includes employer contributions, supplemental contributions, and reemployed annuitant employer contributions.


## Notes to Schedule of Contributions

| Valuation Date: | June 30, 2016 |
| :--- | :--- |
| Notes | Actuarially determined contribution rates are calculated as of each July 1. |

Methods and Assumptions Used to Determine Contribution Rates:

| Actuarial Cost Method | Entry Age Normal |
| :--- | :--- |
| Amortization Method | Level Percentage of Payroll, Closed |
| Remaining Amortization Period | 26 years |
| Asset Valuation Method | 5 -Year smoothed market; no corridor |
| Inflation | $3.00 \%$ |
| Salary Increases | $4.00 \%$ to $8.90 \%$; age and service based |
| Investment Rate of Return | $8.00 \%$ |
| Retirement Age | Experience-based table of rates that are specific to the type of eligibility condition. Last |
|  | updated for the 2012 valuation pursuant to an experience study of the period 2006 - <br>  <br> Mortality |
|  | 2011. <br>  |
|  | fr-2000 Combined Mortality Table, projected with scale AA to 2020, set back one year |
|  |  |

## Other Information:

Notes
The plan is assumed to pay a 2.0\% COLA beginning January 1, 2055, and a 2.5\% COLA beginning January 1, 2066.
See separate funding report as of July 1, 2016 for additional detail.

## Schedule of Investment Returns Multiyear

## Last 10 Fiscal Years (to be completed prospectively, commencing with 2014)



St. Paul Teachers’ Retirement Fund Association compiled this data and the related investment notes and furnished this information for inclusion within this report. We did not audit this information. We are not responsible for its accuracy or completeness.

## Rate of Return

The Association’s money-weighted rate of return for the year ending June 30, 2016 was $0.34 \%$ (net of investment expenses). The money-weighted rate of return expresses investment performance, net of investment expenses, adjusted for the actual cash flows that took place during the performance period.

## 10-Year Schedule of Money-Weighted Investment Return

This schedule is presented to illustrate the requirement to show information for 10 years. However, until a full 10-year trend is compiled, SPTRFA will present information for those years for which information is available.

## SECTION D

NOTES TO FINANCIAL STATEMENTS

Note - Section D is intended to assist in preparation of the financial statements of the St. Paul Teachers' Retirement Fund Association. Financial statements are the responsibility of management, subject to the auditor's review.

## Long-Term Expected Return on Plan Assets

The long-term expected rate of return on pension plan investments was determined using a building-block method in which expected future real rates of return (expected returns, net of pension plan investment expense and inflation) are developed for each major asset class. These real rates of return are combined to produce the long-term expected rate of return by weighting the expected future real rates of return by the target asset allocation percentage and by adding expected inflation. For each major asset class that is included in the pension plan's target asset allocation as of June 30, 2016, these best estimates are summarized in the following table:

## Long-Term Expected Real Rate of Return*

| Asset Class | Target Allocation | Long-Term Expected <br> Real Rate of Return <br> (Arithmetic) |
| :---: | :---: | :---: |
| Domestic Equity | 35\% | 6.55\% |
| International Equity | 20\% | 6.98\% |
| Fixed Income | 20\% | 3.45\% |
| Real Assets | 11\% | 3.90\% |
| Private Equity \& Alternatives | 9\% | 7.47\% |
| Opportunistic | 5\% | 6.08\% |
| Total | 100\% |  |

St. Paul Teachers’ Retirement Fund Association compiled this data and the related investment notes and furnished this information for inclusion within this report. We did not audit this information. We are not responsible for its accuracy or completeness.

## Single Discount Rate

A Single Discount Rate of $8.00 \%$ was used to measure the total pension liability. This Single Discount Rate was based on the expected rate of return on pension plan investments of $8.00 \%$. The projection of cash flows used to determine this Single Discount Rate assumed that plan member contributions will be made at the current contribution rate and that employer contributions will be made at rates equal to the difference between actuarially determined contribution rates and the member rate. Based on these assumptions, the pension plan's fiduciary net position was projected to be available to make all projected future benefit payments of current plan members. Therefore, the long-term expected rate of return on pension plan investments was applied to all periods of projected benefit payments to determine the total pension liability.

Regarding the sensitivity of the net pension liability to changes in the Single Discount Rate, the following presents the plan’s net pension liability, calculated using a Single Discount Rate of $8.00 \%$, as well as what the plan's net pension liability would be if it were calculated using a Single Discount Rate that is one percent lower or one percent higher:

## Sensitivity of Net Pension Liability

to the Single Discount Rate Assumption
(Dollars in Thousands)

|  | Current Single Discount |  |  |
| :--- | :---: | :---: | :---: |
|  | $\mathbf{1 \%}$ Decrease | Rate Assumption | $\mathbf{1 \%}$ Increase |
|  | $\mathbf{7 . 0 0 \%}$ | $\mathbf{8 . 0 0 \%}$ | $\mathbf{9 . 0 0 \%}$ |
| Total Pension Liability | $\$ 1,763,823$ | $\$ 1,592,570$ | $\$ 1,449,234$ |
| Net Position Restricted for Pensions | 959,666 | 959,666 | 959,666 |
| Net Pension Liability | $\$ \mathbf{8 0 4 , 1 5 7}$ | $\mathbf{\$ 6 3 2 , 9 0 4}$ | $\mathbf{\$ 4 8 9 , 5 6 8}$ |

## Reconciliation of Members

## Summary of Changes in Participant Status <br> During Fiscal Year Ending June 30, 2016

| Active | Leave of | Vested | Other | Retired |  | Survivors and Alternate |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Participants | Absence | Terminated | Non-Vested | Participants | Disableds | Beneficiaries | Payees $^{2}$ |


| A. Number as of June 30, 2015 | 3,597 | 159 | 1,892 | 1,981 | 3,238 | 32 | 323 | 40 | 11,262 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B. Additions | 280 | 59 | 220 | 246 | 158 | 2 | 32 |  | 997 |
| C. Deletions |  |  |  |  |  |  |  |  |  |
| 1. Retirements | (88) | (8) | (55) | (5) |  |  |  |  | (156) |
| 2. Disability | - | (1) | (1) |  |  |  |  |  | (2) |
| 3. Died with Beneficiary |  |  |  |  | (31) | (1) |  |  | (32) |
| 4. Died without Beneficiary | (1) | (2) | (3) | (3) | (41) | (1) | (25) |  | (76) |
| 5. Terminated - Deferred | (194) | (26) |  |  |  |  |  |  | (220) |
| 6. Terminated - Not Vested | (235) | (6) |  |  |  |  |  |  | (241) |
| 7. Refunds | (30) |  | (10) | (71) |  |  |  |  | (111) |
| 8. Rehired as Active | 173 | (96) | (27) | (50) |  |  |  |  | 0 |
| 9. Leave of Absence | (45) |  | (11) |  |  |  |  |  | (56) |
| 10. Repayment of Refund |  |  | 1 |  |  |  |  |  | 1 |
| 11. Expired Benefits |  |  |  |  |  |  | (2) |  | (2) |
| 12. Disability to Retirement |  |  |  |  |  | (1) |  |  | (1) |
| D. Data Adjustments ${ }^{1}$ | (2) |  | 14 | 817 |  |  |  |  | 829 |
| E. Total on June 30, 2016 | 3,455 | 79 | 2,020 | 2,915 | 3,324 | 31 | 328 | 40 | 12,192 |

${ }^{1}$ Includes members not valued in prior valuation who repaid refunds or otherwise restored prior service.
${ }^{2}$ Includes alternate payees of both retired participants and disabled participants.

## GASB RECONCILIATION (DOLLARS IN THOUSANDS)

Fiscal Year Ended June 30, 2016

| Balance Beginning of Year | Total Pension Liability <br> (a) |  | Plan Fiduciary Net Position <br> (b) |  | Net Pension Liability (a) - (b) |  | Deferred Outflows |  | Deferred Inflows |  | Net Deferred Outflows Prior Year |  | Total <br> Pension Expense |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Changes for the Year: |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Service Cost | \$ | 25,596 |  |  | \$ | 25,596 |  |  |  |  |  |  | \$ | 25,596 |
| Interest on Total Pension Liability |  | 124,294 |  |  |  | 124,294 |  |  |  |  |  |  |  | 124,294 |
| Interest on Fiduciary Net Position ${ }^{(1)}$ |  |  | \$ | 78,926 |  | $(78,926)$ |  |  |  |  |  |  |  | $(78,926)$ |
| Changes in Benefit Terms |  | - |  |  |  | - |  |  |  |  |  |  |  | - |
| Liability Experience Gains and Losses |  | $(42,295)$ |  |  |  | $(42,295)$ |  |  | \$ | 48,504 | \$ | $(23,461)$ |  | $(17,252)$ |
| Changes in Assumptions |  |  |  |  |  |  | \$ | 15,858 |  |  |  | 23,786 |  | 7,928 |
| Contributions - Employer |  |  |  | 37,228 |  | $(37,228)$ |  |  |  |  |  |  |  | - |
| Contributions - Employees |  |  |  | 18,538 |  | $(18,538)$ |  |  |  |  |  |  |  | $(18,538)$ |
| Asset Gain/(Loss) ${ }^{(1)}$ |  |  |  | $(77,451)$ |  | 77,451 |  | 95,338 |  | 38,304 |  | $(12,954)$ |  | 7,463 |
| Benefit Payouts |  | $(111,795)$ |  | $(111,795)$ |  |  |  |  |  |  |  |  |  | - |
| Administrative Expenses |  |  |  | (749) |  | 749 |  |  |  |  |  |  |  | 749 |
| Other changes |  |  |  |  |  |  |  |  |  |  |  |  | \$ | - |
| Net Changes | \$ | $(4,200)$ | \$ | $(55,303)$ | \$ | 51,103 | \$ | 111,196 | \$ | 86,808 | \$ | $(12,629)$ | \$ | 51,314 |
| Balance End of Year | \$ | 1,592,570 | \$ | 959,666 | \$ | 632,904 | \$ | 111,196 | \$ | 86,808 |  |  |  |  |

${ }^{(1)}$ The sum of these items equals the net investment income of $\$ 1,475$.

## SECTION E

SUMMARY OF BENEFITS

## Summary of Benefit Provisions for Basic Members

## STATUTORY CONTRIBUTIONS

Statutory contribution rates for members and their employers are shown as a percent of pay below:

| Contribution After June 30, | Member | Employer <br> Regular | Employer <br> Additional |  |
| :---: | :---: | :---: | :---: | :---: |
| 2014 | $9.00 \%$ | $9.00 \%$ | $3.64 \%$ <br> 2015 | $9.50 \%$ |
| 2016 | $10.00 \%$ | $9.50 \%$ | $3.64 \%$ |  |
| 2017 | $10.00 \%$ | $9.75 \%$ | $3.64 \%$ |  |
|  |  | $10.00 \%$ | $3.64 \%$ |  |

## PARTICIPANTS

Professional Educators first employed prior to July 1, 1978 by schools in the City of St. Paul or St. Paul College whose position requires a license from the Minnesota Department of Education, who are not covered under the Social Security Act.

## ACCREDITED SERVICE

Service which has been verified and accredited by the Association for the purpose of determining contributions and benefits (may include service earned while working outside of St. Paul Public Schools, previous St. Paul service, military service and governmental service).

## ALLOWABLE ST. PAUL SERVICE

Service earned as a licensed educator in the St. Paul Public Schools, in the St. Paul College, or as an employee of the Association. Also includes service credited after receipt of payment as required, for licensed educators on leave.

## SALARY

Total compensation earned during a school year (July 1 to June 30) excluding lump sum payments for unused leave at termination and employer-paid insurance coverage.

## AVERAGE SALARY

Average of the highest five years of salary during the last 10 years of St. Paul service while making contributions or while disabled.

## NORMAL RETIREMENT BENEFIT

## Eligibility

Attainment of age 65 and 5 years of Accredited Service.

## Benefit

2.50\% of Average Salary for each year of Accredited Service.

## Summary of Benefit Provisions for Basic Members

## EARLY RETIREMENT BENEFIT

## Eligibility

Attainment of age 55 and 5 years of Accredited Service.

## Benefit

The greater of the following benefits:

- 2.00 percent of Average Salary per year of Accredited Service, subject to a maximum of 40 years with a $0.25 \%$ reduction for each month the member is under age 65 . If the member has 25 years of Accredited Service, the reduction is taken from age 60, therefore no reduction is required if the member is age 60 or older. No reduction is taken if age plus years of Accredited Service totals at least 90.
- 2.50 percent of Average Salary per year of Accredited Service, subject to a maximum of 40 years, reduced for each month the member is under age 65 using linear interpolation of the table listed below.

| Age at Retirement | Under Age 62 <br> or less than 30 <br> years of service |  | Age $\mathbf{6 2}$ or older <br> with $\mathbf{3 0}$ years of <br> service |
| :---: | :---: | :---: | :---: |
| $\mathbf{5 5}$ | 0.5376 |  |  |
| $\mathbf{5 6}$ | 0.5745 |  |  |
| $\mathbf{5 7}$ | 0.6092 |  |  |
| $\mathbf{5 8}$ | 0.6419 |  |  |
| $\mathbf{5 9}$ | 0.6726 |  |  |
| $\mathbf{6 0}$ | 0.7354 |  |  |
| $\mathbf{6 1}$ | 0.7947 |  |  |
| $\mathbf{6 2}$ | 0.8507 |  |  |
| $\mathbf{6 3}$ | 0.9035 | 0.8831 |  |
| $\mathbf{6 4}$ | 0.9533 | 0.9246 |  |
| $\mathbf{6 5}$ | 1.0000 | 0.9635 |  |
|  |  | 1.0000 |  |

## DISABILITY RETIREMENT BENEFIT

## Eligibility

Total and permanent disablement before attaining age 65 and 5 years of Accredited Service.

## Benefit

If the member is under age 65, 75 percent of the member's annual contract salary less any Social Security and Workers' Compensation benefits payable until age 65. At age 65, a normal retirement benefit is calculated using the projected service and average salary as if the member had continued to teach in their position held at the time of disability. Members age 65 or older at time of disability receive a normal retirement benefit.

## Summary of Benefit Provisions for Basic Members

## DEFERRED RETIREMENT BENEFIT

## Eligibility

5 years of Accredited Service.

## Benefit

Benefit computed under law in effect at termination and payable as a normal or early retirement benefit. For members hired on or before June 30, 2006, the benefit is augmented at 3.00 percent compounded annually from the $1^{\text {st }}$ of the month following termination until the January $1^{\text {st }}$ after turning age 55 and then augmented at 5.00 percent compounded annually from that date to July 1, 2012. For members hired after June 30, 2006, the benefit is augmented at 2.50 percent compounded annually from the $1^{\text {st }}$ of the month following termination to July 1, 2012. Augmentation for all members, regardless of hire date, changed to 2.00 percent as of July 1, 2012 for the portion of benefit deferral which occurs after June 30, 2012.

## ACTIVE SURVIVOR BENEFIT (Family Benefit)

Eligibility
Active member with three years of Accredited Service.

## Benefit

- Children's Benefit: 25 percent of the maximum Bachelor of Arts salary for the year in which the member died for each eligible child up to a maximum of two. Benefits are paid until the child attains age 18, or 22 for full-time students.
- Spousal Benefit: 15 percent of the maximum Bachelor of Arts salary for an eligible spouse who has legal custody of an eligible child. Spousal benefits cease when the spouse remarries, dies, or elects the regular survivor benefit. Electing the regular survivor benefit does not disqualify the child from receiving the family benefit.


## SURVIVOR BENEFIT (Active or Retired Member)

## Eligibility

Active member or retired member with five years of Accredited Service. A surviving spouse must have been married to the member for three years at the earlier of the member's death or retirement.

## Benefit

Retirement benefit earned at the time of death or retirement, whichever is earlier, reduced by the use of one hundred percent joint survivorship tables, based on the ages of the member and survivor at the time of retirement.

## Summary of Benefit Provisions for Basic Members

## REFUND OF CONTRIBUTIONS

## Eligibility

Termination or death where no annuity is payable, or prior to age 55, if a refund of contributions is chosen in lieu of an annuity.

## Benefit

Member contributions with 6.00 percent interest accrued before July 1, 2011, with 4.00 percent accrual thereafter.

## NORMAL FORM OF RETIREMENT BENEFITS

Unreduced annuity payments made until the death of the member, with a 100 percent Joint \& Survivor adjusted pension payable to the surviving beneficiary.

## BENEFIT INCREASES

If the Accrued Liability Funding Ratio, based on Actuarial Value of Assets, as determined by the two consecutive and most recent actuarial valuations are:

Less than 80 percent for two consecutive years, the COLA: 1.00 percent
Between 80 percent and 90 percent for two consecutive years, the COLA: 2.00 percent
If at least 90 percent for two consecutive years, the COLA: 2.50 percent

## Summary of Benefit Provisions for Coordinated Members

## STATUTORY CONTRIBUTIONS

Statutory contribution rates for members and their employers are shown as a percent of pay below.

| Contribution After June 30, |  | Member | Employer <br> Regular | Employer <br> Additional |
| :---: | :---: | :---: | :---: | :---: |
| 2014 |  | $6.50 \%$ |  | $5.50 \%$ |
| 2015 | $7.00 \%$ |  | $3.00 \%$ | $3.84 \%$ |
| 2016 | $7.50 \%$ | $6.25 \%$ | $3.84 \%$ |  |
| 2017 | $7.50 \%$ | $6.50 \%$ | $3.84 \%$ |  |

## PARTICIPANTS

Professional educators in the public schools of the City of St. Paul, excluding charter schools, whose position requires a license from the Minnesota Department of Education, and who are covered under the Social Security Act and make contributions to the St. Paul Teachers’ Retirement Fund Association, are covered under the Coordinated Plan.

## ALLOWABLE SERVICE

Service earned as a licensed educator in the St. Paul Public Schools, in the St. Paul College, or in certain charter schools, or as an employee of the Association. Also includes service credited after receipt of payment as required, for licensed educators on leave. Service is granted on a proportional basis for part-time teachers.

## SALARY

Total compensation excluding lump sum payments for unused leave at termination and employerpaid insurance coverage.

## AVERAGE SALARY

Average of the highest five successive years of salary while making contributions. In cases where the Allowable Service is less than five years, Average Salary is based on the Allowable Service years.

## NORMAL RETIREMENT BENEFIT

## Eligibility

Three years of Allowable Service. The eligibility age is 65 for those hired before July 1, 1989, and the earlier of eligibility for full Social Security retirement benefits to a maximum of age 66 for those hired on or after July 1, 1989. A Proportionate Retirement Annuity is available at Normal Retirement Age with one year of Allowable Service.

## Benefit

1.70 percent of Average Salary for each year of Allowable Service rendered before July 1, 2015 and 1.90 percent of Average Salary for each year of Allowable Service rendered after June 30, 2015.

# Summary of Benefit Provisions for Coordinated Members 

## EARLY RETIREMENT BENEFIT

## Eligibility

Attainment of age 55 and 3 years of Allowable Service.

## Benefit

Members hired before July 1, 1989, are eligible for the greater of the following benefits. Members hired after July 1, 1989, are eligible for the benefits shown in item (b):
a) For the first ten years of Allowable Service, 1.20 percent of Average Salary for each year of Allowable Service rendered prior to July 1, 2015, plus 1.40 percent of Average Salary for each year of Allowable Service rendered after June 30, 2015. Additionally, for each subsequent year of Allowable Service in excess of ten years, 1.70 percent of Average Salary for each year rendered prior to July 1, 2015, plus 1.90 percent of Average Salary for each year rendered after June 30, 2015. There is a reduction of 0.25 percent for each month the member is under age 65, or under age 62 with 30 years of Allowable Service. No reduction applies if the age plus years of service totals at least 90 .
b) 1.70 percent of Average Salary per year of Allowable Service rendered before July 1, 2015 and 1.90 percent of Average Salary for each year of service rendered after June 30, 2015 reduced for each month the member is under the Normal Retirement Age using linear interpolation of the factors in the table listed below.

| Normal retirement age:Age at Retirement | Under Age 62 or less than 30 years of service |  | Age 62 or older with 30 years of service |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 65 | 66 | 65 | 66 |
|  |  |  |  |  |
| 55 | 0.5376 | 0.4592 |  |  |
| 56 | 0.5745 | 0.4992 |  |  |
| 57 | 0.6092 | 0.5370 |  |  |
| 58 | 0.6419 | 0.5726 |  |  |
| 59 | 0.6726 | 0.6062 |  |  |
| 60 | 0.7354 | 0.6726 |  |  |
| 61 | 0.7947 | 0.7354 |  |  |
| 62 | 0.8507 | 0.7947 | 0.8831 | 0.8389 |
| 63 | 0.9035 | 0.8507 | 0.9246 | 0.8831 |
| 64 | 0.9533 | 0.9035 | 0.9635 | 0.9246 |
| 65 | 1.0000 | 0.9533 | 1.0000 | 0.9635 |
| 66 |  | 1.0000 |  | 1.0000 |

## Summary of Benefit Provisions for Coordinated Members

## DISABILITY RETIREMENT BENEFIT

## Eligibility

Total and permanent disablement and three years of Allowable Service with service earned within the current fiscal year and at least two years of Allowable Service since the last interruption in service.

## Benefit

Calculated as a normal retirement benefit payable for life without reduction for early commencement. At normal retirement age, the benefit converts from a disability benefit to a retirement benefit. The disability benefit is reduced by any Workers' Compensation benefits payable.

## DEFERRED RETIREMENT BENEFIT

## Eligibility

Three years of Allowable Service.

## Benefit

Benefit computed under law in effect at termination and payable as a normal or early retirement benefit. For members hired on or before June 30, 2006, the benefit is augmented at 3.00 percent compounded annually from the $1^{\text {st }}$ of the month following termination until the January $1^{\text {st }}$ after turning age 55 and then augmented at 5.00 percent compounded annually from that date to July 1, 2012. For members hired after June 30, 2006, the benefit is augmented at 2.50 percent compounded annually from the $1^{\text {st }}$ of the month following termination to July 1, 2012. Augmentation for all members, regardless of hire date, changed to 2.00 percent as of July 1, 2012 for the portion of benefit deferral which occurs after June 30, 2012.

## Summary of Benefit Provisions for Coordinated Members

## SURVIVOR BENEFIT (Active Members)

## Eligibility

Active member with three years of Allowable service. A surviving spouse is defined as the person legally married to the member at the time of death. If none, a dependent child who is the legal child of the member, who is less than 20 years of age and unmarried.

## Benefit

Retirement benefit earned at the time of death with choices for either a reduced for 100 percent joint survivorship, or $5-$ - $10-$ - 15 -, or 20 -year term certain. The benefit is available immediately upon application. Actuarial reductions assuming 2.5\% augmentation for the calculation of the survivorship portion of a 100 percent joint and survivor benefit are actuarially determined based on the member's and survivor's ages at the death of the member.

Early retirement reductions apply to the survivor benefit based on the member's age when deceased. If the deceased member had not yet attained age 55 at time of death, the additional early retirement reduction from age 55 to the age of the member at death applies at only one-half of the actuarial rate.

## REFUND OF CONTRIBUTIONS

## Eligibility

Termination or death where no annuity is payable or a refund of contributions is chosen in lieu of an annuity.

## Benefit

Member contributions with 6.00 percent interest accrued until July 1, 2011, with 4.00 percent accrual thereafter.

## NORMAL FORM OF RETIREMENT BENEFITS

Straight life annuity. Actuarially equivalent options are available to provide post-retirement beneficiary or survivor benefits.

## BENEFIT INCREASES

If the Accrued Liability Funding Ratio, based on Actuarial Value of Assets, as determined by the two consecutive and most recent actuarial valuations are:

Less than 80 percent for two consecutive years, the COLA: 1.00 percent Between 80 percent and 90 percent for two consecutive years, the COLA: 2.00 percent If at least 90 percent for two consecutive years, the COLA: 2.50 percent

## SECTION F

ACTUARIAL COST METHOD AND ACTUARIAL ASSUMPTIONS

## I. ACTUARIAL METHODS

## Actuarial Cost Method

Normal cost and the allocation of benefit values between service rendered before and after the valuation date were determined using an Individual Entry-Age Actuarial Cost Method having the following characteristics:
(i) the annual normal cost for each individual active member, payable from the date of employment to the date of retirement, is sufficient to accumulate the value of the member's benefit at the time of retirement; and
(ii) each annual normal cost is a constant percentage of the member's year by year projected covered pay.
Actuarial gains/(losses), as they occur, reduce (increase) the Unfunded Actuarial Accrued Liability.

## Asset Value

Fair market value.

## Valuation of Future COLAs

Benefit recipients receive a future annual 1.0\% COLA. If the funding ratio reaches $80 \%$ for two consecutive years, the COLA will increase to $2.0 \%$. If the funding ratio reaches $90 \%$ for two consecutive years, the COLA will increase to $2.5 \%$.

To determine an assumption regarding a future change in the COLA, we performed a projection of liabilities and assets based on the following methods and assumptions:

- Future investment returns of $8.00 \%$
- Liabilities and normal cost based on statutory funding assumptions
o Discount rate of $8.00 \%$
o Statutory salary increases
- Open group; stable active population (new member profile based on average new members hired in recent years)
- The COLA is assumed to be $1.00 \%$ per year until the funding ratio thresholds required to pay $2.00 \%$ or $2.50 \%$ are reached

Based on these assumptions and methods, the July 1, 2016 projection indicates that this plan is expected to attain the funding ratio threshold required to pay a $2 \%$ COLA beginning January 1 , 2055; and a $2.5 \%$ COLA beginning January 1, 2066. These assumptions are reflected in our calculations.

## II. CURRENT ACTUARIAL ASSUMPTIONS

The assumptions were last updated for the July 1, 2013 valuation as a result of an experience study during the five-year period of July 1, 2006 to June 30, 2011, as well as a legislated change to the investment return assumption effective July 1, 2015.

## A. Demographic Assumptions

Mortality:

1. Healthy Mortality*:
a. Male: RP-2000 Combined Mortality Table for males projected with Scale AA to 2020 set back 1 year
b. Female: RP-2000 Combined Mortality Table for females projected with Scale AA to 2020 set back 3 years
2. Disabled Mortality:
a. Male: RP-2000 Disabled Life Mortality Table for males
b. Female: RP-2000 Disabled Life Mortality Table for females

* Mortality rates were adjusted to include margin for future mortality improvement as described in the table name above.

Deaths Expressed as the Number of Occurrences per 10,000:

| Age | Healthy <br> Mortality |  | Disabled <br> Mortality |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Male | Female | Male | Female |
| 20 | 2 | 1 | 226 | 75 |
| 21 | 2 | 1 | 226 | 75 |
| 22 | 2 | 1 | 226 | 75 |
| 23 | 3 | 1 | 226 | 75 |
| 24 | 3 | 1 | 226 | 75 |
| 25 | 3 | 1 | 226 | 75 |
| 26 | 3 | 1 | 226 | 75 |
| 27 | 3 | 1 | 226 | 75 |
| 28 | 3 | 2 | 226 | 75 |
| 29 | 4 | 2 | 226 | 75 |
| 30 | 4 | 2 | 226 | 75 |
| 31 | 4 | 2 | 226 | 75 |
| 32 | 5 | 2 | 226 | 75 |
| 33 | 5 | 2 | 226 | 75 |
| 34 | 6 | 3 | 226 | 75 |
| 35 | 6 | 3 | 226 | 75 |
| 36 | 7 | 3 | 226 | 75 |
| 37 | 8 | 4 | 226 | 75 |
| 38 | 8 | 4 | 226 | 75 |
| 39 | 9 | 4 | 226 | 75 |
| 40 | 9 | 4 | 226 | 75 |
| 41 | 9 | 5 | 226 | 75 |
| 42 | 10 | 5 | 226 | 75 |
| 43 | 10 | 5 | 226 | 75 |
| 44 | 10 | 6 | 226 | 75 |

Deaths Expressed as the Number of Occurrences per 10,000:

| Age | Healthy <br> Mortality |  | Disabled <br> Mortality |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Male | Female | Male | Female |
| 45 | 11 | 6 | 226 | 75 |
| 46 | 12 | 7 | 238 | 82 |
| 47 | 12 | 8 | 251 | 90 |
| 48 | 13 | 8 | 264 | 98 |
| 49 | 13 | 9 | 277 | 106 |
| 50 | 14 | 9 | 290 | 115 |
| 51 | 15 | 10 | 303 | 125 |
| 52 | 17 | 11 | 316 | 135 |
| 53 | 18 | 12 | 329 | 145 |
| 54 | 19 | 13 | 342 | 155 |
| 55 | 21 | 15 | 354 | 165 |
| 56 | 25 | 17 | 367 | 176 |
| 57 | 29 | 20 | 380 | 187 |
| 58 | 33 | 23 | 393 | 197 |
| 59 | 38 | 27 | 407 | 208 |
| 60 | 43 | 31 | 420 | 218 |
| 61 | 49 | 35 | 435 | 229 |
| 62 | 57 | 40 | 450 | 241 |
| 63 | 65 | 46 | 466 | 253 |
| 64 | 76 | 53 | 483 | 266 |
| 65 | 85 | 60 | 502 | 280 |
| 66 | 96 | 69 | 522 | 296 |
| 67 | 111 | 78 | 545 | 313 |
| 68 | 124 | 88 | 569 | 332 |
| 69 | 135 | 99 | 596 | 353 |

Rates of Disability:

Disability Expressed as the Number of Occurrences per 10,000:

| Age | Disability | Age | Disability |
| :---: | :---: | :---: | :---: |
| 20 | 2 | 45 | 5 |
| 21 | 2 | 46 | 5 |
| 22 | 2 | 47 | 5 |
| 23 | 2 | 48 | 5 |
| 24 | 2 | 49 | 5 |
| 25 | 2 | 50 | 10 |
| 26 | 2 | 51 | 10 |
| 27 | 2 | 52 | 10 |
| 28 | 2 | 53 | 10 |
| 29 | 2 | 54 | 10 |
| 30 | 3 | 55 | 20 |
| 31 | 3 | 56 | 20 |
| 32 | 3 | 57 | 20 |
| 33 | 3 | 58 | 20 |
| 34 | 3 | 59 | 20 |
| 35 | 3 | 60 | 40 |
| 36 | 3 | 61 | 40 |
| 37 | 3 | 62 | 40 |
| 38 | 3 | 63 | 40 |
| 39 | 3 | 64 | 40 |
| 40 | 3 |  |  |
| 41 | 3 |  |  |
| 42 | 3 |  |  |
| 43 | 3 |  |  |
| 44 | 3 |  |  |

Rates of Termination:

| Years of <br> Service |  | Number of Terminations <br> per 1,000 Active Members |  |
| :---: | :---: | :---: | :---: |
|  |  | Male |  |

## Rates of Retirement:

Retirements Expressed as the Number of Occurrences per 10,000:

| Age | Basic Members Eligible for Rule of 90 Provision | Basic Members Not Eligible for Rule of 90 Provision | Male Coordinated Members Eligible for Rule of 90 Provision | Female Coordinated Members Eligible for Rule of 90 | Male Coordinated Members Not Eligible for Rule of 90 Provision | Female Coordinated Members Not Eligible for Rule of 90 Provision |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 55 | 5,000 | 800 | 3,500 | 3,500 | 700 | 500 |
| 56 | 5,000 | 1,300 | 3,500 | 3,500 | 700 | 500 |
| 57 | 4,000 | 1,300 | 3,500 | 3,500 | 700 | 500 |
| 58 | 4,000 | 1,800 | 3,500 | 3,500 | 700 | 500 |
| 59 | 3,500 | 1,800 | 3,500 | 3,500 | 700 | 500 |
| 60 | 3,500 | 2,000 | 3,500 | 3,500 | 1,100 | 800 |
| 61 | 3,500 | 2,000 | 3,500 | 3,500 | 1,500 | 1,100 |
| 62 | 3,500 | 4,000 | 3,500 | 3,500 | 1,900 | 1,400 |
| 63 | 3,500 | 4,000 | 3,500 | 3,500 | 2,300 | 1,900 |
| 64 | 4,000 | 4,000 | 3,500 | 4,000 | 2,700 | 2,400 |
| 65 | 5,000 | 5,000 | 3,500 | 5,000 | 3,100 | 3,500 |
| 66 | 3,000 | 5,000 | 3,500 | 5,000 | 3,500 | 3,500 |
| 67 | 3,000 | 5,000 | 3,500 | 5,000 | 3,500 | 3,500 |
| 68 | 3,000 | 5,000 | 3,500 | 5,000 | 3,500 | 3,500 |
| 69 | 3,000 | 5,000 | 3,500 | 5,000 | 3,500 | 3,500 |
| 70 \& Over | 10,000 | 10,000 | 10,000 | 10,000 | 10,000 | 10,000 |

## B. Economic Assumptions

Investment Return Rate: 8.00\%
Cost-of-Living Increases: 1.00\% per year through 2054; 2.00\% beginning 2055; 2.50\% beginning 2066.

Wage Inflation: $\quad$ 4.00\% per annum
Future Salary Increases: In addition to the age-based rates shown below, during the first 15 years of employment, a service-based component of $0.20 \%$ x $(15-\mathrm{T})$, where T is completed years of service, is included in the salary increase used.

Annual Salary Increases

| Age | Ulimate Rate of Annual Salary Increases | Age | Ultimate Rate of Annual Salary Increases |
| :---: | :---: | :---: | :---: |
| <22 | 5.90\% | 45 | 4.75\% |
| 23 | 5.85 | 46 | 4.70 |
| 24 | 5.80 | 47 | 4.65 |
|  |  | 48 | 4.60 |
| 25 | 5.75 | 49 | 4.55 |
| 26 | 5.70 |  |  |
| 27 | 5.65 | 50 | 4.50 |
| 28 | 5.60 | 51 | 4.45 |
| 29 | 5.55 | 52 | 4.40 |
|  |  | 53 | 4.35 |
| 30 | 5.50 | 54 | 4.30 |
| 31 | 5.45 |  |  |
| 32 | 5.40 | 55 | 4.25 |
| 33 | 5.35 | 56 | 4.20 |
| 34 | 5.30 | 57 | 4.15 |
|  |  | 58 | 4.10 |
| 35 | 5.25 | 59 | 4.05 |
| 36 | 5.20 |  |  |
| 37 | 5.15 | 60 \& Over | 4.00 |
| 38 | 5.10 |  |  |
| 39 | 5.05 |  |  |
| 40 | 5.00 |  |  |
| 41 | 4.95 |  |  |
| 42 | 4.90 |  |  |
| 43 | 4.85 |  |  |
| 44 | 4.80 |  |  |

## C. Other Assumptions

Marital Status:
Deferred Benefit
Commencement:
Administrative Expenses:
Allowance for Combined Service Annuity:

Missing Salary and Salary Minimums:

Missing Data for Deferred Vested Members:

Decrement Timing:

It is assumed that $75 \%$ of male members and $60 \%$ of female members have an eligible spouse. The male spouse is assumed to be two years older than the female spouse. Married members are assumed to have two dependent children.

Basic Plan members who terminate vested are assumed to commence benefits at age 61. Coordinated Plan members are assumed to commence benefits at age 62. If the member is already past the assumed deferral age, the member is assumed to commence benefits one year from the valuation date.

Prior year administrative expenses (excluding investment expenses) are expressed as a percentage of payroll and then applied to current projected payroll.
7.00\% load on liabilities for active members hired before July 1, 1989;
2.00\% load on liabilities for active members hired after June 30, 1989; and
$30.00 \%$ load on liabilities for former members.
Active members with reported salaries of $\$ 100$ or less were assumed to have the average non-zero active salary. Active members with salaries less than those reported at the prior valuation date are valued using their prior salary amount. Active members who have been hired within one year of the valuation date have had their pay annualized by dividing by months of service credited, not to exceed the average non-zero active salary. For members on leave of absence at valuation date who were not on leave at the prior valuation date, the prior year's valuation pay was used.

Deferred vested members without salary information were assumed to have a final average salary of $\$ 40,000$.

Retirement and Termination: end of valuation year - consistent with retirements and terminations occurring at the end of the school year.

Death and Disability: middle of valuation year.

Valuation of Future Post- If the plan has reached the funding ratio threshold required to pay Retirement Benefit Increases: a different benefit increase, Minnesota Statutes require the benefit increase rate to be reflected in the liability calculations. If the plan has not yet reached the funding ratio threshold required to pay a benefit increase, Minnesota Statutes require a projection to be performed to determine the expected attainment of the funding ratio thresholds, and the expected payment of benefit increases must be reflected in the liability calculations.

Supplemental Contributions: 1996 legislation provides for a variable amortization aid contribution paid annually on July 15 . We assumed the annual amortization aid contribution will equal $\$ 838,000$, which was the actual contribution for the most recent fiscal year. Additionally, according to 1997 legislation, annual supplemental contributions currently equal to $\$ 2,827,000$ are scheduled to be paid on October 1. According to 2014 legislation, the State of Minnesota will make annual additional supplemental contributions of \$7,000,000 on October 1. The contributions described herein will continue until the plan is $100 \%$ funded or until June 30, 2042, whichever occurs earlier.

The census data as of July 1, 2016 reflects retirements and terminations occurring during the months of May and June; however, it does not necessarily reflect the replacements hired to fill their positions who may have hire dates in August and September. We assumed that May and June retirements are replaced by members coming in at the B.A. Step 1 salary level of $\$ 44,759$; and the Projected Annual Payroll for the fiscal year ending June 30, 2016 includes this replacement salary amount.

## SECTION G

CALCULATION OF THE SINGLE DISCOUNT RATE

## Calculation of the Single Discount Rate

GASB Statement No. 67 includes a specific requirement for the discount rate that is used for the purpose of the measurement of the Total Pension Liability. This rate considers the ability of the fund to meet benefit obligations in the future. To make this determination, employer contributions, employee contributions, benefit payments, expenses and investment returns are projected into the future. The Plan Net Position (assets) in future years can then be determined and compared to its obligation to make benefit payments in those years. As long as assets are projected to be on hand in a future year, the assumed valuation discount rate is used. In years where assets are not projected to be sufficient to meet benefit payments, the use of a municipal bond rate is required, as described in the following paragraph. As in 2015, the plan is projected to have sufficient assets to pay all benefits.

The Single Discount Rate (SDR) is equivalent to applying these two rates to the benefits that are projected to be paid during the different time periods. The SDR reflects (1) the long-term expected rate of return on pension plan investments (during the period in which the fiduciary net position is projected to be sufficient to pay benefits) and (2) tax-exempt municipal bond rate based on an index of 20-year general obligation bonds with an average AA credit rating as of the measurement date (to the extent that the contributions for use with the long-term expected rate of return are not met).

For the purpose of this valuation, the expected rate of return on pension plan investments is $8.00 \%$; the municipal bond rate is $2.85 \%$; and the resulting Single Discount Rate is $8.00 \%$.

The tables in this section provide background for the development of the Single Discount Rate.
The Projection of Contributions table shows the development of expected contributions in future years. Normal Cost contributions for future hires are not included (nor are their liabilities).

The Projection of Plan Fiduciary Net Position table shows the development of expected asset levels in future years.

The Present Values of Projected Benefit Payments table shows the development of the Single Discount Rate (SDR). It breaks down the benefit payments into present values for funded and unfunded portions and shows the equivalent total using the SDR.

# Single Discount Rate Development Projection of Contributions (Dollars in Thousands) 

| Year | Payroll |  |  | Projected Contributions |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Payroll for Current Employees | Payroll for New Employees | Total Employee Payroll | Contributions from Current Employees | Employer Contributions for Current Employees | Employer Contributions on Future Payroll toward Current UAL* | Supplemental Contributions | Total Contributions |
| 0 | \$ 258,787 | \$ - | \$ 258,787 |  |  |  |  |  |
| 1 | 271,781 | - | 271,781 | \$ 20,384 | 27,423 | \$ | 10,665 | \$ 58,472 |
| 2 | 262,200 | 20,452 | 282,652 | 19,665 | 27,112 | 1,779 | 10,665 | 59,221 |
| 3 | 256,210 | 37,748 | 293,958 | 19,216 | 26,492 | 3,284 | 10,665 | 59,657 |
| 4 | 251,503 | 54,214 | 305,717 | 18,863 | 26,005 | 4,717 | 10,665 | 60,250 |
| 5 | 247,232 | 70,713 | 317,945 | 18,542 | 25,564 | 6,152 | 10,665 | 60,923 |
| 6 | 243,424 | 87,239 | 330,663 | 18,257 | 25,170 | 7,590 | 10,665 | 61,682 |
| 7 | 240,469 | 103,421 | 343,890 | 18,035 | 24,864 | 8,998 | 10,665 | 62,562 |
| 8 | 237,893 | 119,752 | 357,645 | 17,842 | 24,598 | 10,418 | 10,665 | 63,523 |
| 9 | 235,330 | 136,621 | 371,951 | 17,650 | 24,333 | 11,886 | 10,665 | 64,534 |
| 10 | 232,791 | 154,038 | 386,829 | 17,459 | 24,071 | 13,401 | 10,665 | 65,596 |
| 11 | 229,916 | 172,386 | 402,302 | 17,244 | 23,773 | 14,998 | 10,665 | 66,680 |
| 12 | 226,733 | 191,661 | 418,394 | 17,005 | 23,444 | 16,675 | 10,665 | 67,789 |
| 13 | 223,015 | 212,115 | 435,130 | 16,726 | 23,060 | 18,454 | 10,665 | 68,905 |
| 14 | 218,473 | 234,062 | 452,535 | 16,385 | 22,590 | 20,363 | 10,665 | 70,003 |
| 15 | 213,110 | 257,527 | 470,637 | 15,983 | 22,036 | 22,405 | 10,665 | 71,089 |
| 16 | 206,978 | 282,484 | 489,462 | 15,523 | 21,402 | 24,576 | 10,665 | 72,166 |
| 17 | 200,051 | 308,990 | 509,041 | 15,004 | 20,685 | 26,882 | 10,665 | 73,236 |
| 18 | 192,341 | 337,061 | 529,402 | 14,426 | 19,888 | 29,324 | 10,665 | 74,303 |
| 19 | 183,989 | 366,589 | 550,578 | 13,799 | 19,024 | 31,893 | 10,665 | 75,381 |
| 20 | 175,043 | 397,558 | 572,601 | 13,128 | 18,099 | 34,588 | 10,665 | 76,480 |
| 21 | 165,799 | 429,706 | 595,505 | 12,435 | 17,144 | 37,384 | 10,665 | 77,628 |
| 22 | 156,235 | 463,091 | 619,326 | 11,718 | 16,155 | 40,289 | 10,665 | 78,827 |
| 23 | 146,393 | 497,706 | 644,099 | 10,979 | 15,137 | 43,300 | 10,665 | 80,081 |
| 24 | 136,446 | 533,417 | 669,863 | 10,233 | 14,109 | 46,407 | 10,665 | 81,414 |
| 25 | 126,310 | 570,347 | 696,657 | 9,473 | 13,060 | 49,620 | 10,665 | 82,818 |
| 26 | 116,251 | 608,272 | 724,523 | 8,719 | 12,020 | 52,920 | 10,665 | 84,324 |
| 27 | 106,125 | 647,379 | 753,504 | 7,959 | 10,973 | 56,322 | 10,665 | 85,919 |
| 28 | 95,999 | 687,646 | 783,645 | 7,200 | 9,926 | 59,825 | - | 76,951 |
| 29 | 85,898 | 729,092 | 814,990 | 6,442 | 8,882 | 63,431 | - | 78,755 |
| 30 | 75,974 | 771,616 | 847,590 | 5,698 | 7,856 | 67,131 | - | 80,685 |
| 31 | 66,370 | 815,124 | 881,494 | 4,978 | 6,863 | 70,916 | - | 82,757 |
| 32 | 57,184 | 859,569 | 916,753 | 4,289 | 5,913 | 74,783 | - | 84,985 |
| 33 | 48,441 | 904,982 | 953,423 | 3,633 | 5,009 | 78,733 | - | 87,375 |
| 34 | 40,268 | 951,292 | 991,560 | 3,020 | 4,164 | 82,762 | - | 89,946 |
| 35 | 32,711 | 998,512 | 1,031,223 | 2,453 | 3,382 | 86,871 | - | 92,706 |
| 36 | 25,805 | 1,046,667 | 1,072,472 | 1,935 | 2,668 | 91,060 | - | 95,663 |
| 37 | 19,866 | 1,095,505 | 1,115,371 | 1,490 | 2,054 | 95,309 | - | 98,853 |
| 38 | 14,749 | 1,145,236 | 1,159,985 | 1,106 | 1,525 | 99,636 | - | 102,267 |
| 39 | 10,439 | 1,195,946 | 1,206,385 | 783 | 1,079 | 104,047 | - | 105,909 |
| 40 | 7,026 | 1,247,614 | 1,254,640 | 527 | 726 | 108,542 | - | 109,795 |
| 41 | 4,496 | 1,300,330 | 1,304,826 | 337 | 465 | 113,129 | - | 113,931 |
| 42 | 2,791 | 1,354,228 | 1,357,019 | 209 | 289 | 117,818 | - | 118,316 |
| 43 | 1,604 | 1,409,696 | 1,411,300 | 120 | 166 | 122,644 | - | 122,930 |
| 44 | 820 | 1,466,932 | 1,467,752 | 62 | 85 | 127,623 | - | 127,770 |
| 45 | 362 | 1,526,100 | 1,526,462 | 27 | 37 | 132,771 | - | 132,835 |
| 46 | 126 | 1,587,394 | 1,587,520 | 9 | 13 | 138,103 | - | 138,125 |
| 47 | 33 | 1,650,988 | 1,651,021 | 2 | 3 | 143,636 | - | 143,641 |
| 48 | - | 1,717,062 | 1,717,062 | - | - | 149,384 | - | 149,384 |
| 49 | - | 1,785,744 | 1,785,744 | - | - | 155,360 | - | 155,360 |
| 50 | - | 1,857,174 | 1,857,174 | - | - | 161,574 | - | 161,574 |
| Con | ributions rela | ated to future | employees in | cess of norma | cost and exp | penses of $9.14 \%$ | f pay. |  |

For purposes of this projection, based on GASB guidance, we assumed the statutory contribution rates would continue after the plan becomes fully funded. If we reflected a decrease in contribution rates due to full funding, future assets and contributions would be less than what is shown herein.

# Single Discount Rate Development Projection of Contributions (Concluded) (Dollars in Thousands) 

| Year | Payroll |  |  | Projected Contributions |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Payroll for Current Employees | Payroll for New Employees | $\begin{gathered} \text { Total Employee } \\ \text { Payroll } \\ \hline \end{gathered}$ | Contributions from Current Employees | Employer Contributions for Current Employees | Employer Contributions on Future Payroll toward Current UAL* | Supplemental Contributions | Total Contributions |
| 51 | \$ | 1,931,461 | \$ 1,931,461 | \$ | \$ | \$ 168,037 | \$ - | \$ 168,037 |
| 52 | - | 2,008,719 | 2,008,719 | - | - | 174,759 | - | 174,759 |
| 53 | - | 2,089,068 | 2,089,068 | - | - | 181,749 | - | 181,749 |
| 54 | - | 2,172,631 | 2,172,631 | - | - | 189,019 | - | 189,019 |
| 55 | - | 2,259,536 | 2,259,536 | - | - | 196,580 | - | 196,580 |
| 56 | - | 2,349,918 | 2,349,918 | - | - | 204,443 |  | 204,443 |
| 57 | - | 2,443,914 | 2,443,914 | - | - | 212,621 | - | 212,621 |
| 58 | - | 2,541,671 | 2,541,671 | - | - | 221,125 | - | 221,125 |
| 59 | - | 2,643,338 | 2,643,338 | - | - | 229,970 | - | 229,970 |
| 60 | - | 2,749,071 | 2,749,071 | - | - | 239,169 | - | 239,169 |
| 61 | - | 2,859,034 | 2,859,034 | - | - | 248,736 | - | 248,736 |
| 62 | - | 2,973,396 | 2,973,396 | - | - | 258,685 | - | 258,685 |
| 63 | - | 3,092,331 | 3,092,331 | - | - | 269,033 | - | 269,033 |
| 64 | - | 3,216,025 | 3,216,025 | - | - | 279,794 | - | 279,794 |
| 65 | - | 3,344,666 | 3,344,666 | - | - | 290,986 | - | 290,986 |
| 66 | - | 3,478,452 | 3,478,452 | - | - | 302,625 | - | 302,625 |
| 67 | - | 3,617,590 | 3,617,590 | - | - | 314,730 |  | 314,730 |
| 68 | - | 3,762,294 | 3,762,294 | - | - | 327,320 | - | 327,320 |
| 69 | - | 3,912,786 | 3,912,786 | - | - | 340,412 | - | 340,412 |
| 70 | - | 4,069,297 | 4,069,297 | - | - | 354,029 | - | 354,029 |
| 71 | - | 4,232,069 | 4,232,069 | - | - | 368,190 | - | 368,190 |
| 72 | - | 4,401,352 | 4,401,352 | - | - | 382,918 | - | 382,918 |
| 73 | - | 4,577,406 | 4,577,406 | - | - | 398,234 | - | 398,234 |
| 74 | - | 4,760,502 | 4,760,502 | - | - | 414,164 | - | 414,164 |
| 75 | - | 4,950,922 | 4,950,922 | - | - | 430,730 | - | 430,730 |
| 76 | - | 5,148,959 | 5,148,959 | - | - | 447,959 | - | 447,959 |
| 77 | - | 5,354,917 | 5,354,917 | - | - | 465,878 | - | 465,878 |
| 78 | - | 5,569,114 | 5,569,114 | - | - | 484,513 | - | 484,513 |
| 79 | - | 5,791,879 | 5,791,879 | - | - | 503,893 | - | 503,893 |
| 80 | - | 6,023,554 | 6,023,554 | - | - | 524,049 | - | 524,049 |
| 81 | - | 6,264,496 | 6,264,496 | - | - | 545,011 | - | 545,011 |
| 82 | - | 6,515,076 | 6,515,076 | - | - | 566,812 | - | 566,812 |
| 83 | - | 6,775,679 | 6,775,679 | - | - | 589,484 | - | 589,484 |
| 84 | - | 7,046,706 | 7,046,706 | - | - | 613,063 | - | 613,063 |
| 85 | - | 7,328,574 | 7,328,574 | - | - | 637,586 | - | 637,586 |
| 86 | - | 7,621,717 | 7,621,717 | - | - | 663,089 | - | 663,089 |
| 87 | - | 7,926,586 | 7,926,586 | - | - | 689,613 | - | 689,613 |
| 88 | - | 8,243,649 | 8,243,649 | - | - | 717,197 | - | 717,197 |
| 89 | - | 8,573,395 | 8,573,395 | - | - | 745,885 | - | 745,885 |
| 90 | - | 8,916,331 | 8,916,331 | - | - | 775,721 | - | 775,721 |
| 91 | - | 9,272,984 | 9,272,984 | - | - | 806,750 | - | 806,750 |
| 92 | - | 9,643,904 | 9,643,904 | - | - | 839,020 | - | 839,020 |
| 93 | - | 10,029,660 | 10,029,660 | - | - | 872,580 | - | 872,580 |
| 94 | - | 10,430,846 | 10,430,846 | - | - | 907,484 | - | 907,484 |
| 95 | - | 10,848,080 | 10,848,080 | - | - | 943,783 | - | 943,783 |
| 96 | - | 11,282,003 | 11,282,003 | - | - | 981,534 | - | 981,534 |
| 97 | - | 11,733,283 | 11,733,283 | - | - | 1,020,796 | - | 1,020,796 |
| 98 | - | 12,202,615 | 12,202,615 | - | - | 1,061,627 | - | 1,061,627 |
| 99 | - | 12,690,719 | 12,690,719 | - | - | 1,104,093 | - | 1,104,093 |
| 100 |  | 13,198,348 | 13,198,348 | - | - | 1,148,256 | - | 1,148,256 |
| Co | ibutions rel | ed to future | mployees in | cess of norm | al cost and exp | enses of $9.14 \%$ | of pay. |  |

For purposes of this projection, based on GASB guidance, we assumed the statutory contribution rates would continue after the plan becomes fully funded. If we reflected a decrease in contribution rates due to full funding, future assets and contributions would be less than what is shown herein.

# Single Discount Rate Development Projection of Plan Fiduciary Net Position (Dollars in Thousands) 

| Year | Projected Beginning Plan Net Position | Projected Total Contributions | Projected Benefit Payments | Projected Administrative Expenses | Projected Investment Earnings at $8.00 \%$ | Projected Ending Plan Net Position |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (a) | (b) | (c) | (d) | (e) | (f)=(a)+(b)-(c)-(d)+(e) |
| 1 | \$ 959,666 | \$ 58,472 | \$ 115,345 | \$ 734 | 74,513 | 976,572 |
| 2 | 976,572 | 59,221 | 118,455 | 708 | 75,774 | 992,404 |
| 3 | 992,404 | 59,657 | 121,343 | 692 | 76,945 | 1,006,971 |
| 4 | 1,006,971 | 60,250 | 123,942 | 679 | 78,032 | 1,020,632 |
| 5 | 1,020,632 | 60,923 | 126,550 | 668 | 79,050 | 1,033,387 |
| 6 | 1,033,387 | 61,682 | 128,977 | 657 | 80,005 | 1,045,440 |
| 7 | 1,045,440 | 62,562 | 130,834 | 649 | 80,931 | 1,057,450 |
| 8 | 1,057,450 | 63,523 | 132,572 | 642 | 81,862 | 1,069,621 |
| 9 | 1,069,621 | 64,534 | 134,165 | 635 | 82,813 | 1,082,168 |
| 10 | 1,082,168 | 65,596 | 135,544 | 629 | 83,805 | 1,095,396 |
| 11 | 1,095,396 | 66,680 | 137,044 | 621 | 84,847 | 1,109,258 |
| 12 | 1,109,258 | 67,789 | 138,594 | 612 | 85,939 | 1,123,780 |
| 13 | 1,123,780 | 68,905 | 140,198 | 602 | 87,082 | 1,138,967 |
| 14 | 1,138,967 | 70,003 | 142,039 | 590 | 88,268 | 1,154,609 |
| 15 | 1,154,609 | 71,089 | 144,224 | 575 | 89,477 | 1,170,376 |
| 16 | 1,170,376 | 72,166 | 146,595 | 559 | 90,688 | 1,186,076 |
| 17 | 1,186,076 | 73,236 | 149,427 | 540 | 91,876 | 1,201,221 |
| 18 | 1,201,221 | 74,303 | 152,414 | 519 | 93,013 | 1,215,604 |
| 19 | 1,215,604 | 75,381 | 155,451 | 497 | 94,088 | 1,229,125 |
| 20 | 1,229,125 | 76,480 | 158,735 | 473 | 95,085 | 1,241,482 |
| 21 | 1,241,482 | 77,628 | 162,038 | 448 | 95,990 | 1,252,614 |
| 22 | 1,252,614 | 78,827 | 165,457 | 422 | 96,794 | 1,262,356 |
| 23 | 1,262,356 | 80,081 | 168,705 | 395 | 97,497 | 1,270,834 |
| 24 | 1,270,834 | 81,414 | 171,783 | 368 | 98,107 | 1,278,204 |
| 25 | 1,278,204 | 82,818 | 174,940 | 341 | 98,629 | 1,284,370 |
| 26 | 1,284,370 | 84,324 | 177,723 | 314 | 99,074 | 1,289,731 |
| 27 | 1,289,731 | 85,919 | 180,496 | 287 | 99,457 | 1,294,324 |
| 28 | 1,294,324 | 76,951 | 183,341 | 259 | 99,362 | 1,287,037 |
| 29 | 1,287,037 | 78,755 | 185,963 | 232 | 98,748 | 1,278,345 |
| 30 | 1,278,345 | 80,685 | 188,327 | 205 | 98,037 | 1,268,535 |
| 31 | 1,268,535 | 82,757 | 190,573 | 179 | 97,247 | 1,257,787 |
| 32 | 1,257,787 | 84,985 | 192,623 | 154 | 96,394 | 1,246,389 |
| 33 | 1,246,389 | 87,375 | 194,333 | 131 | 95,510 | 1,234,810 |
| 34 | 1,234,810 | 89,946 | 195,394 | 109 | 94,644 | 1,223,897 |
| 35 | 1,223,897 | 92,706 | 196,077 | 88 | 93,853 | 1,214,291 |
| 36 | 1,214,291 | 95,663 | 196,298 | 70 | 93,193 | 1,206,779 |
| 37 | 1,206,779 | 98,853 | 195,558 | 54 | 92,747 | 1,202,767 |
| 38 | 1,202,767 | 102,267 | 193,886 | 40 | 92,626 | 1,203,734 |
| 39 | 1,203,734 | 105,909 | 191,368 | 28 | 92,946 | 1,211,193 |
| 40 | 1,211,193 | 109,795 | 189,701 | 19 | 93,761 | 1,225,029 |
| 41 | 1,225,029 | 113,931 | 187,056 | 12 | 95,134 | 1,247,026 |
| 42 | 1,247,026 | 118,316 | 183,540 | 8 | 97,204 | 1,278,998 |
| 43 | 1,278,998 | 122,930 | 179,365 | 4 | 100,106 | 1,322,665 |
| 44 | 1,322,665 | 127,770 | 174,602 | 2 | 103,976 | 1,379,807 |
| 45 | 1,379,807 | 132,835 | 169,308 | 1 | 108,954 | 1,452,287 |
| 46 | 1,452,287 | 138,125 | 163,568 | - | 115,185 | 1,542,029 |
| 47 | 1,542,029 | 143,641 | 157,453 | - | 122,821 | 1,651,038 |
| 48 | 1,651,038 | 149,384 | 151,052 | - | 132,018 | 1,781,388 |
| 49 | 1,781,388 | 155,360 | 144,405 | - | 142,941 | 1,935,284 |
| 50 | 1,935,284 | 161,574 | 137,584 | - | 155,764 | 2,115,038 |

For purposes of this projection, based on GASB guidance, we assumed the statutory contribution rates would continue after the plan becomes fully funded. If we reflected a decrease in contribution rates due to full funding, future assets and contributions would be less than what is shown herein.

# Single Discount Rate Development Projection of Plan Fiduciary Net Position (Concluded) (Dollars in Thousands) 

| Year | ProjectedBeginning Plan Net Position | Projected Total Contributions | Projected Benefit Payments | Projected Administrative Expenses | $\begin{gathered} \text { Projected } \\ \text { Investment } \\ \text { Earnings at } 8.00 \% \end{gathered}$ |  | Projected Ending Plan <br> Net Position |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (a) | (b) | (c) | (d) | (e) |  | (f)=(a)+(b)-(c)-(d)+(e) |
| 51 | \$ 2,115,038 | \$ 168,037 | \$ 131,224 | \$ | \$ 170,648 | \$ | 2,322,499 |
| 52 | 2,322,499 | 174,759 | 124,666 | - | 187,766 |  | 2,560,358 |
| 53 | 2,560,358 | 181,749 | 117,945 | - | 207,332 |  | 2,831,494 |
| 54 | 2,831,494 | 189,019 | 111,096 | - | 229,577 |  | 3,138,994 |
| 55 | 3,138,994 | 196,580 | 104,154 | - | 254,746 |  | 3,486,166 |
| 56 | 3,486,166 | 204,443 | 97,158 | - | 283,103 |  | 3,876,554 |
| 57 | 3,876,554 | 212,621 | 90,152 | - | 314,929 |  | 4,313,952 |
| 58 | 4,313,952 | 221,125 | 83,180 | - | 350,528 |  | 4,802,425 |
| 59 | 4,802,425 | 229,970 | 76,281 | - | 390,224 |  | 5,346,338 |
| 60 | 5,346,338 | 239,169 | 69,502 | - | 434,364 |  | 5,950,369 |
| 61 | 5,950,369 | 248,736 | 62,888 | - | 483,321 |  | 6,619,538 |
| 62 | 6,619,538 | 258,685 | 56,484 | - | 537,496 |  | 7,359,235 |
| 63 | 7,359,235 | 269,033 | 50,331 | - | 597,319 |  | 8,175,256 |
| 64 | 8,175,256 | 279,794 | 44,472 | - | 663,253 |  | 9,073,831 |
| 65 | 9,073,831 | 290,986 | 38,947 | - | 735,795 |  | 10,061,665 |
| 66 | 10,061,665 | 302,625 | 33,790 | - | 815,481 |  | 11,145,981 |
| 67 | 11,145,981 | 314,730 | 29,031 | - | 902,887 |  | 12,334,567 |
| 68 | 12,334,567 | 327,320 | 24,692 | - | 998,639 |  | 13,635,834 |
| 69 | 13,635,834 | 340,412 | 20,786 | - | 1,103,407 |  | 15,058,867 |
| 70 | 15,058,867 | 354,029 | 17,313 | - | 1,217,920 |  | 16,613,503 |
| 71 | 16,613,503 | 368,190 | 14,264 | - | 1,342,966 |  | 18,310,395 |
| 72 | 18,310,395 | 382,918 | 11,625 | - | 1,479,398 |  | 20,161,086 |
| 73 | 20,161,086 | 398,234 | 9,373 | - | 1,628,143 |  | 22,178,090 |
| 74 | 22,178,090 | 414,164 | 7,475 | - | 1,790,203 |  | 24,374,982 |
| 75 | 24,374,982 | 430,730 | 5,897 | - | 1,966,666 |  | 26,766,481 |
| 76 | 26,766,481 | 447,959 | 4,603 | - | 2,158,712 |  | 29,368,549 |
| 77 | 29,368,549 | 465,878 | 3,555 | - | 2,367,622 |  | 32,198,494 |
| 78 | 32,198,494 | 484,513 | 2,716 | - | 2,594,781 |  | 35,275,072 |
| 79 | 35,275,072 | 503,893 | 2,052 | - | 2,841,694 |  | 38,618,607 |
| 80 | 38,618,607 | 524,049 | 1,531 | - | 3,109,988 |  | 42,251,113 |
| 81 | 42,251,113 | 545,011 | 1,127 | - | 3,401,427 |  | 46,196,424 |
| 82 | 46,196,424 | 566,812 | 818 | - | 3,717,919 |  | 50,480,337 |
| 83 | 50,480,337 | 589,484 | 585 | - | 4,061,531 |  | 55,130,767 |
| 84 | 55,130,767 | 613,063 | 411 | - | 4,434,497 |  | 60,177,916 |
| 85 | 60,177,916 | 637,586 | 284 | - | 4,839,236 |  | 65,654,454 |
| 86 | 65,654,454 | 663,089 | 192 | - | 5,278,363 |  | 71,595,714 |
| 87 | 71,595,714 | 689,613 | 128 | - | 5,754,707 |  | 78,039,906 |
| 88 | 78,039,906 | 717,197 | 83 | - | 6,271,326 |  | 85,028,346 |
| 89 | 85,028,346 | 745,885 | 53 | - | 6,831,528 |  | 92,605,706 |
| 90 | 92,605,706 | 775,721 | 33 | - | 7,438,888 |  | 100,820,282 |
| 91 | 100,820,282 | 806,750 | 20 | - | 8,097,272 |  | 109,724,284 |
| 92 | 109,724,284 | 839,020 | 12 | - | 8,810,858 |  | 119,374,150 |
| 93 | 119,374,150 | 872,580 | 7 | - | 9,584,164 |  | 129,830,887 |
| 94 | 129,830,887 | 907,484 | 3 | - | 10,422,073 |  | 141,160,441 |
| 95 | 141,160,441 | 943,783 | 1 | - | 11,329,861 |  | 153,434,084 |
| 96 | 153,434,084 | 981,534 | - | - | 12,313,234 |  | 166,728,852 |
| 97 | 166,728,852 | 1,020,796 | - | - | 13,378,355 |  | 181,128,003 |
| 98 | 181,128,003 | 1,061,627 | - | - | 14,531,889 |  | 196,721,519 |
| 99 | 196,721,519 | 1,104,093 | - | - | 15,781,037 |  | 213,606,649 |
| 100 | 213,606,649 | 1,148,256 | - | - | 17,133,579 |  | 231,888,484 |

For purposes of this projection, based on GASB guidance, we assumed the statutory contribution rates would continue after the plan becomes fully funded. If we reflected a decrease in contribution rates due to full funding, future assets and contributions would be less than what is shown herein.

# Single Discount Rate Development Present Values of Projected Benefits (Dollars in Thousands) 

| Year | Projected Beginning Plan Net Position | Projected Benefit Payments | Funded Portion of Benefit Payments | Unfunded Portion of Benefit Payments | Present Value of Funded Benefit Payments using Expected Return Rate (v) | Present Value of Unfunded Benefit Payments using Municipal Bond Rate (v) | Present Value of Benefit Payments using Single Discount Rate (sdr) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | (b) | (c) | (d) | (e) | (f)=(d)*v^((a)-.5) | (g)=(e)*vf $\wedge($ (a)-.5) | (h)=((c)/( $1+\mathrm{sdr})^{\wedge}(\mathrm{a}-5)$ |
| 1 | \$ 959,666 | \$ 115,345 | 115,345 | \$ | \$ 110,991 | \$ - | \$ 110,991 |
| 2 | 976,571 | 118,455 | 118,455 | - | 105,540 | - | 105,540 |
| 3 | 992,404 | 121,343 | 121,343 | - | 100,105 | - | 100,105 |
| 4 | 1,006,971 | 123,942 | 123,942 | - | 94,675 | - | 94,675 |
| 5 | 1,020,632 | 126,550 | 126,550 | - | 89,507 |  | 89,507 |
| 6 | 1,033,388 | 128,977 | 128,977 | - | 84,466 | - | 84,466 |
| 7 | 1,045,441 | 130,834 | 130,834 | - | 79,335 | - | 79,335 |
| 8 | 1,057,451 | 132,572 | 132,572 | - | 74,434 | - | 74,434 |
| 9 | 1,069,623 | 134,165 | 134,165 | - | 69,749 | - | 69,749 |
| 10 | 1,082,169 | 135,544 | 135,544 | - | 65,246 | - | 65,246 |
| 11 | 1,095,398 | 137,044 | 137,044 | - | 61,082 | - | 61,082 |
| 12 | 1,109,260 | 138,594 | 138,594 | - | 57,197 | - | 57,197 |
| 13 | 1,123,781 | 140,198 | 140,198 | - | 53,573 | - | 53,573 |
| 14 | 1,138,968 | 142,039 | 142,039 | - | 50,256 | - | 50,256 |
| 15 | 1,154,611 | 144,224 | 144,224 | - | 47,249 | - | 47,249 |
| 16 | 1,170,377 | 146,595 | 146,595 | - | 44,468 | - | 44,468 |
| 17 | 1,186,077 | 149,427 | 149,427 | - | 41,970 | - | 41,970 |
| 18 | 1,201,223 | 152,414 | 152,414 | - | 39,638 | - | 39,638 |
| 19 | 1,215,605 | 155,451 | 155,451 | - | 37,433 | - | 37,433 |
| 20 | 1,229,127 | 158,735 | 158,735 | - | 35,392 | - | 35,392 |
| 21 | 1,241,485 | 162,038 | 162,038 | - | 33,453 | - | 33,453 |
| 22 | 1,252,618 | 165,457 | 165,457 | - | 31,628 | - | 31,628 |
| 23 | 1,262,360 | 168,705 | 168,705 | - | 29,860 | - | 29,860 |
| 24 | 1,270,837 | 171,783 | 171,783 | - | 28,153 | - | 28,153 |
| 25 | 1,278,208 | 174,940 | 174,940 | - | 26,547 | - | 26,547 |
| 26 | 1,284,374 | 177,723 | 177,723 | - | 24,971 | - | 24,971 |
| 27 | 1,289,735 | 180,496 | 180,496 | - | 23,482 | - | 23,482 |
| 28 | 1,294,329 | 183,341 | 183,341 | - | 22,086 | - | 22,086 |
| 29 | 1,287,042 | 185,963 | 185,963 | - | 20,742 | - | 20,742 |
| 30 | 1,278,351 | 188,327 | 188,327 | - | 19,450 | - | 19,450 |
| 31 | 1,268,541 | 190,573 | 190,573 | - | 18,224 | - | 18,224 |
| 32 | 1,257,791 | 192,623 | 192,623 | - | 17,055 | - | 17,055 |
| 33 | 1,246,392 | 194,333 | 194,333 | - | 15,932 | - | 15,932 |
| 34 | 1,234,814 | 195,394 | 195,394 | - | 14,833 | - | 14,833 |
| 35 | 1,223,902 | 196,077 | 196,077 | - | 13,782 | - | 13,782 |
| 36 | 1,214,296 | 196,298 | 196,298 | - | 12,775 | - | 12,775 |
| 37 | 1,206,785 | 195,558 | 195,558 | - | 11,784 | - | 11,784 |
| 38 | 1,202,774 | 193,886 | 193,886 | - | 10,818 | - | 10,818 |
| 39 | 1,203,741 | 191,368 | 191,368 | - | 9,887 | - | 9,887 |
| 40 | 1,211,200 | 189,701 | 189,701 | - | 9,075 | - | 9,075 |
| 41 | 1,225,036 | 187,056 | 187,056 | - | 8,285 | - | 8,285 |
| 42 | 1,247,032 | 183,540 | 183,540 | - | 7,527 | - | 7,527 |
| 43 | 1,279,004 | 179,365 | 179,365 | - | 6,811 | - | 6,811 |
| 44 | 1,322,671 | 174,602 | 174,602 | - | 6,139 | - | 6,139 |
| 45 | 1,379,812 | 169,308 | 169,308 | - | 5,512 | - | 5,512 |
| 46 | 1,452,292 | 163,568 | 163,568 | - | 4,931 | - | 4,931 |
| 47 | 1,542,036 | 157,453 | 157,453 | - | 4,395 | - | 4,395 |
| 48 | 1,651,045 | 151,052 | 151,052 | - | 3,904 | - | 3,904 |
| 49 | 1,781,396 | 144,405 | 144,405 | - | 3,456 | - | 3,456 |
| 50 | 1,935,292 | 137,584 | 137,584 | - | 3,049 | - | 3,049 |

For purposes of this projection, based on GASB guidance, we assumed the statutory contribution rates would continue after the plan becomes fully funded. If we reflected a decrease in contribution rates due to full funding, future assets and contributions would be less than what is shown herein.

# Single Discount Rate Development Present Values of Projected Benefits (CONCLUded) (DOLLARS IN THOUSANDS) 

| Year | Projected Beginning Plan Net Position | Projected Benefit Payments | Funded Portion of Benefit Payments | Unfunded Portion of Benefit Payments | Present Value of Funded Benefit <br> Payments using Expected Return Rate (v) | Present Value of Unfunded Benefit Payments using Municipal Bond Rate (vf) | Present Value of Benefit <br> Payments using Single Discount Rate (sdr) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | (b) | (c) | (d) | (e) | (f)=(d)*v^((a)-.5) | (g) $=(\mathrm{e}) * \mathrm{vf} \wedge((\mathrm{a})-.5)$ | (h) $=\left((\mathrm{c}) /(1+\mathrm{sdr})^{\wedge}(\mathrm{a}-5)\right.$ |
| 51 | \$ 2,115,046 | 131,224 | \$ 131,224 | \$ | \$ 2,692 | \$ | \$ 2,692 |
| 52 | 2,322,508 | 124,666 | 124,666 | - | 2,368 | - | 2,368 |
| 53 | 2,560,366 | 117,945 | 117,945 | - | 2,075 |  | 2,075 |
| 54 | 2,831,502 | 111,096 | 111,096 | - | 1,809 |  | 1,809 |
| 55 | 3,139,002 | 104,154 | 104,154 | - | 1,571 | - | 1,571 |
| 56 | 3,486,174 | 97,158 | 97,158 | - | 1,357 | - | 1,357 |
| 57 | 3,876,562 | 90,152 | 90,152 | - | 1,166 | - | 1,166 |
| 58 | 4,313,960 | 83,180 | 83,180 | - | 996 | - | 996 |
| 59 | 4,802,434 | 76,281 | 76,281 | - | 846 | - | 846 |
| 60 | 5,346,347 | 69,502 | 69,502 | - | 713 | - | 713 |
| 61 | 5,950,378 | 62,888 | 62,888 | - | 598 | - | 598 |
| 62 | 6,619,547 | 56,484 | 56,484 | - | 497 | - | 497 |
| 63 | 7,359,245 | 50,331 | 50,331 | - | 410 | - | 410 |
| 64 | 8,175,266 | 44,472 | 44,472 | - | 335 | - | 335 |
| 65 | 9,073,842 | 38,947 | 38,947 | - | 272 | - | 272 |
| 66 | 10,061,676 | 33,790 | 33,790 | - | 219 | - | 219 |
| 67 | 11,145,991 | 29,031 | 29,031 | - | 174 | - | 174 |
| 68 | 12,334,579 | 24,692 | 24,692 | - | 137 | - | 137 |
| 69 | 13,635,845 | 20,786 | 20,786 | - | 107 | - | 107 |
| 70 | 15,058,878 | 17,313 | 17,313 | - | 82 | - | 82 |
| 71 | 16,613,514 | 14,264 | 14,264 | - | 63 | - | 63 |
| 72 | 18,310,405 | 11,625 | 11,625 | - | 47 | - | 47 |
| 73 | 20,161,096 | 9,373 | 9,373 | - | 35 | - | 35 |
| 74 | 22,178,101 | 7,475 | 7,475 | - | 26 | - | 26 |
| 75 | 24,374,992 | 5,897 | 5,897 | - | 19 | - | 19 |
| 76 | 26,766,491 | 4,603 | 4,603 | - | 14 | - | 14 |
| 77 | 29,368,559 | 3,555 | 3,555 | - | 10 | - | 10 |
| 78 | 32,198,504 | 2,716 | 2,716 | - | 7 | - | 7 |
| 79 | 35,275,082 | 2,052 | 2,052 | - | 5 | - | 5 |
| 80 | 38,618,618 | 1,531 | 1,531 | - | 3 | - | 3 |
| 81 | 42,251,124 | 1,127 | 1,127 | - | 2 | - | 2 |
| 82 | 46,196,435 | 818 | 818 | - | 2 | - | 2 |
| 83 | 50,480,347 | 585 | 585 | - | 1 | - | 1 |
| 84 | 55,130,778 | 411 | 411 | - | 1 | - | 1 |
| 85 | 60,177,927 | 284 | 284 | - | - | - | - |
| 86 | 65,654,465 | 192 | 192 | - | - | - | - |
| 87 | 71,595,726 | 128 | 128 | - | - | - | - |
| 88 | 78,039,918 | 83 | 83 | - | - | - | - |
| 89 | 85,028,358 | 53 | 53 | - | - | - | - |
| 90 | 92,605,718 | 33 | 33 | - | - | - | - |
| 91 | 100,820,294 | 20 | 20 | - | - | - | - |
| 92 | 109,724,295 | 12 | 12 | - | - | - | - |
| 93 | 119,374,162 | 7 | 7 | - | - | - | - |
| 94 | 129,830,900 | 3 | 3 | - | - | - | - |
| 95 | 141,160,453 | 1 | 1 | - | - | - | - |
| 96 | 153,434,096 | - | - | - | - | - | - |
| 97 | 166,728,863 | - | - | - | - | - | - |
| 98 | 181,128,014 | - | - | - | - | - | - |
| 99 | 196,721,531 | - | - | - | - | - | - |
| 100 | 213,606,660 | - | - | - | - | - | - |
|  |  |  |  | Totals | \$ 1,809,509 | \$ | \$ 1,809,509 |

For purposes of this projection, based on GASB guidance, we assumed the statutory contribution rates would continue after the plan becomes fully funded. If we reflected a decrease in contribution rates due to full funding, future assets and contributions would be less than what is shown herein.

## SECTION H

GLOSSARY OF TERMS

## GLOSSARY OF TERMS

## Actuarial Accrued Liability (AAL)

## Actuarial Assumptions

## Accrued Service

Actuarial Equivalent

## Actuarial Cost Method

## Actuarial Gain (Loss)

## Actuarial Present Value (APV)

## Actuarial Valuation

## Actuarial Valuation Date

Actuarially Determined Contribution (ADC) or Annual Required Contribution (ARC)

The AAL is the difference between the actuarial present value of all benefits and the actuarial value of future normal costs. The definition comes from the fundamental equation of funding which states that the present value of all benefits is the sum of the Actuarial Accrued Liability and the present value of future normal costs. The AAL may also be referred to as "accrued liability" or "actuarial liability."

These assumptions are estimates of future experience with respect to rates of mortality, disability, turnover, retirement, rate or rates of investment income and compensation increases. Actuarial assumptions are generally based on past experience, often modified for projected changes in conditions. Economic assumptions (compensation increases, payroll growth, inflation and investment return) consist of an underlying real rate of return plus an assumption for a long-term average rate of inflation.

Service credited under the system which was rendered before the date of the actuarial valuation.

A single amount or series of amounts of equal actuarial value to another single amount or series of amounts, computed on the basis of appropriate actuarial assumptions.

A mathematical budgeting procedure for allocating the dollar amount of the actuarial present value of the pension trust benefits between future normal cost and actuarial accrued liability. The actuarial cost method may also be referred to as the actuarial funding method.

The difference in liabilities between actual experience and expected experience during the period between two actuarial valuations is the gain (loss) on the accrued liabilities.

The amount of funds currently required to provide a payment or series of payments in the future. The present value is determined by discounting future payments at predetermined rates of interest and probabilities of payment.

The actuarial valuation report determines, as of the actuarial valuation date, the service cost, total pension liability, and related actuarial present value of projected benefit payments for pensions.

The date as of which an actuarial valuation is performed.
A calculated contribution into a defined benefit pension plan for the reporting period, most often determined based on the funding policy of the plan. Typically the Actuarially Determined Contribution has a normal cost payment and an amortization payment.

## GLOSSARY OF TERMS

## Amortization Payment

Amortization Method

Cost-of-Living Adjustments

Cost-Sharing Multiple-
Employer Defined Benefit
Pension Plan (cost-sharing pension plan)

Covered-Employee Payroll

Deferred Retirement Option Program (DROP)

## Deferred Inflows and Outflows

The amortization payment is the periodic payment required to pay off an interest-discounted amount with payments of interest and principal.

The method used to determine the periodic amortization payment may be a level dollar amount, or a level percent of pay amount. The period will typically be expressed in years, and the method will either be "open" (meaning, reset each year) or "closed" (the number of years remaining will decline each year).

Postemployment benefit changes intended to adjust benefit payments for the effects of inflation.

A multiple-employer defined benefit pension plan in which the pension obligations to the employees of more than one employer are pooled and pension plan assets can be used to pay the benefits of the employees of any employer that provides pensions through the pension plan.

The payroll of employees that are provided with pensions through the pension plan.

A program that permits a plan member to elect a calculation of benefit payments based on service credits and salary, as applicable, as of the DROP entry date. The plan member continues to provide service to the employer and is paid for the service by the employer after the DROP entry date; however, the pensions that would have been paid to the plan member are credited to an individual member account within the defined benefit pension plan until the end of the DROP period. Other variations for DROP exist and will be more fully detailed in the plan provision section of the valuation report.

The deferred inflows and outflows of pension resources are amounts used under GASB Statement No. 68 in developing the annual pension expense. Deferred inflows and outflows arise with differences between expected and actual experiences; changes of assumptions. The portion of these amounts not included in pension expense should be included in the deferred inflows or outflows of resources.

For GASB purposes, the discount rate is the single rate of return that results in the present value of all projected benefit payments to be equal to the sum of the funded and unfunded projected benefit payments, specifically:

1. The benefit payments to be made while the pension plans' fiduciary net position is projected to be greater than the benefit payments that are projected to be made in the period; and
2. The present value of the benefit payments not in (1) above, discounted using the municipal bond rate.

## GLOSSARY OF TERMS

## Entry Age Actuarial Cost Method (EAN)

GASB

## Fiduciary Net Position

Long-Term Expected Rate of Return

Money-Weighted Rate of Return

Multiple-Employer Defined
Benefit Pension Plan
Municipal Bond Rate

Net Pension Liability (NPL) The NPL is the liability of employers and non-employer contributing entities to plan members for benefits provided through a defined benefit pension plan.

Non-employer contributing entities are entities that make contributions to a pension plan that is used to provide pensions to the employees of other entities. For purposes of the GASB accounting statements, plan members are not considered non-employer contributing entities.

The portion of the actuarial present value allocated to a valuation year is called the normal cost. For purposes of application to the requirements of this Statement, the term normal cost is the equivalent of service cost.

## Glossary of Terms

Other Postemployment Benefits (OPEB)

Real Rate of Return

Service Cost

Total Pension Expense

All postemployment benefits other than retirement income (such as death benefits, life insurance, disability, and long-term care) that are provided separately from a pension plan, as well as postemployment healthcare benefits regardless of the manner in which they are provided. Other postemployment benefits do not include termination benefits.

The real rate of return is the rate of return on an investment after adjustment to eliminate inflation.

The service cost is the portion of the actuarial present value of projected benefit payments that is attributed to a valuation year.

The total pension expense is the sum of the following items that are recognized at the end of the employer's fiscal year:

1. Service Cost
2. Interest on the Total Pension Liability
3. Current-Period Benefit Changes
4. Employee Contributions (made negative for addition here)
5. Projected Earnings on Plan Investments (made negative for addition here)
6. Pension Plan Administrative Expense
7. Other Changes in Plan Fiduciary Net Position
8. Recognition of Outflow (Inflow) of Resources due to Liabilities
9. Recognition of Outflow (Inflow) of Resources due to Assets

Total Pension Liability (TPL) The TPL is the portion of the actuarial present value of projected benefit payments that is attributed to past periods of member service.

## Unfunded Actuarial Accrued Liability (UAAL)

Valuation Assets

The UAAL is the difference between actuarial accrued liability and valuation assets.

The valuation assets are the assets used in determining the unfunded liability of the plan. For purposes of GASB Statement Nos. 67 and 68, the valuation assets are equal to the market value of assets.


[^0]:    * Based on the Bond Buyer 20-Bond Index of general obligation municipal bonds as of June 30, 2016
    (i.e., the weekly rate closest to but not later than the Measurement Date).

[^1]:    * Includes impact of changes in expected timing of future COLA increases.

